

WIEFP 2022

Principles of

Force and Impedance Control of hydraulically-actuated robots

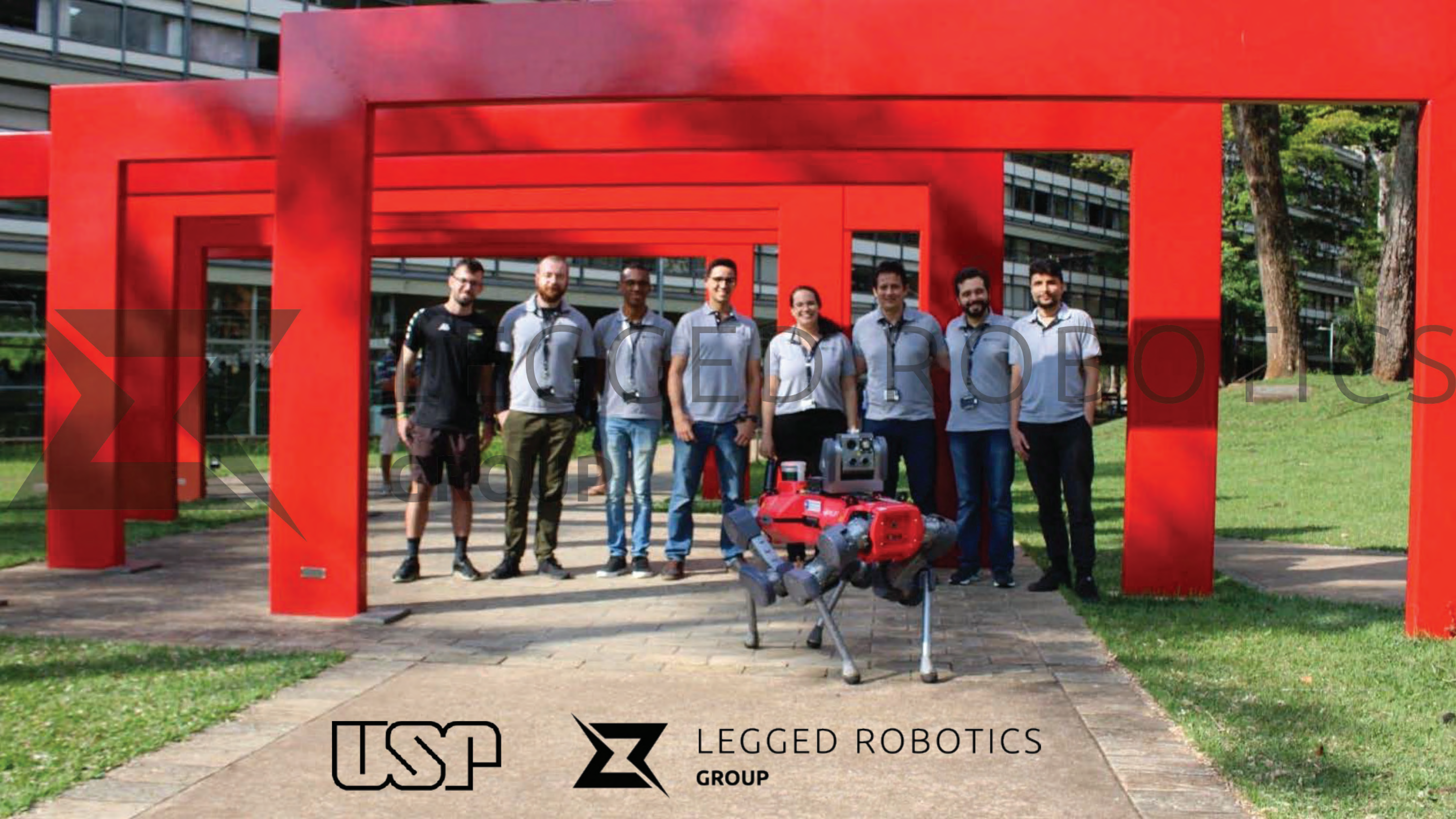
by Prof. Dr. Thiago Boaventura



Universidade de São Paulo
Brasil



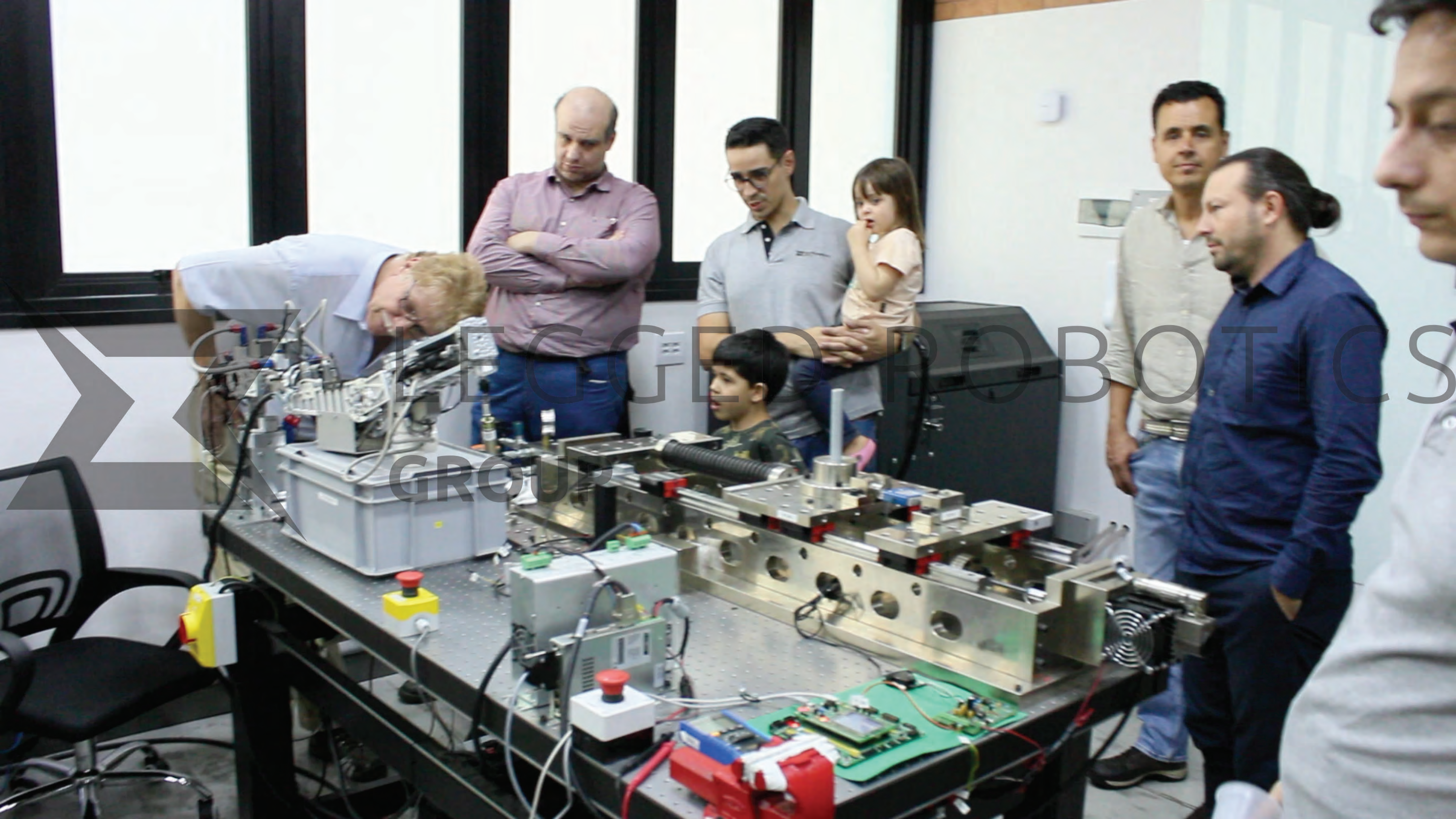
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USP



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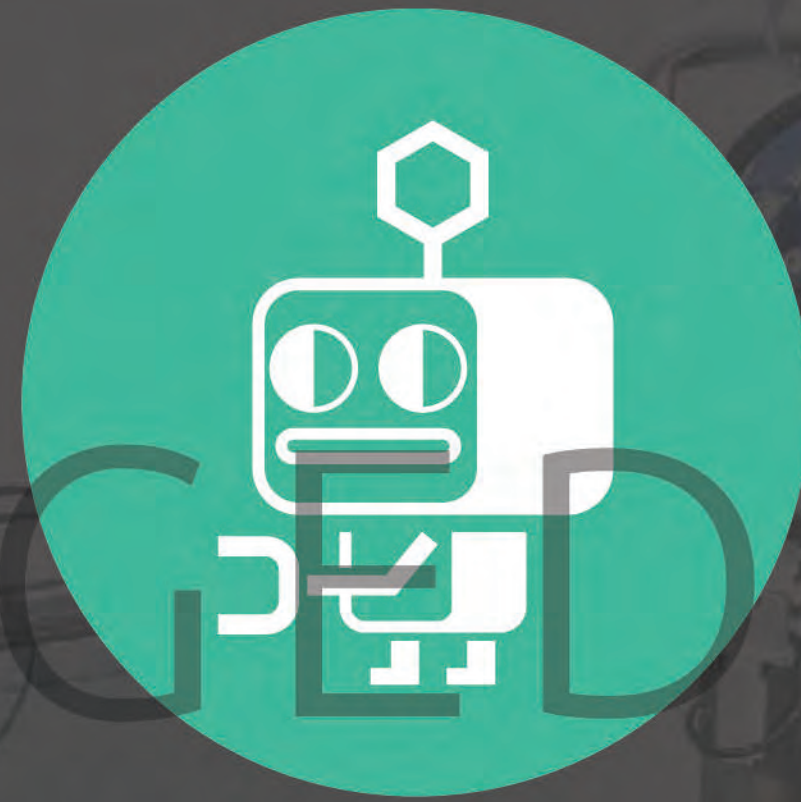
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ROBOTICS

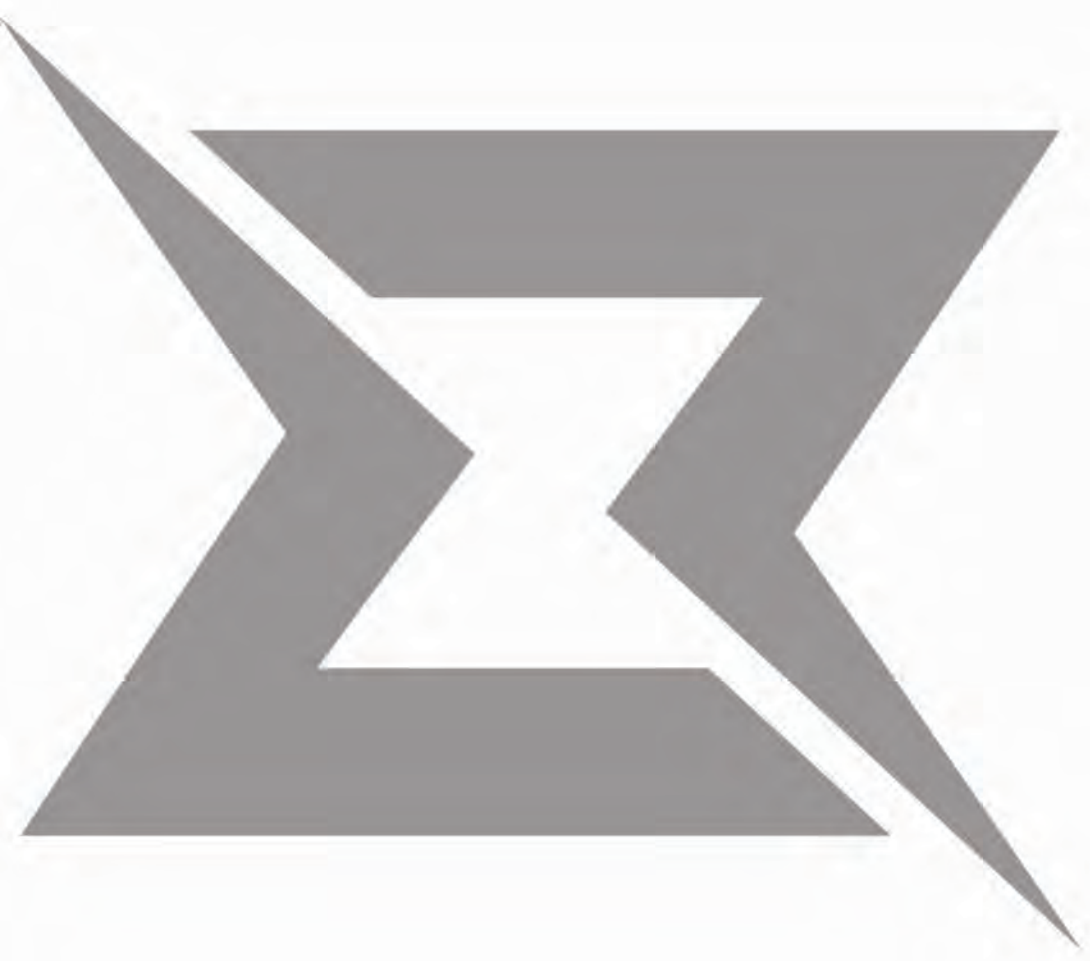
interaction control



basic
principles



impedance
control



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Control of

physical interaction!

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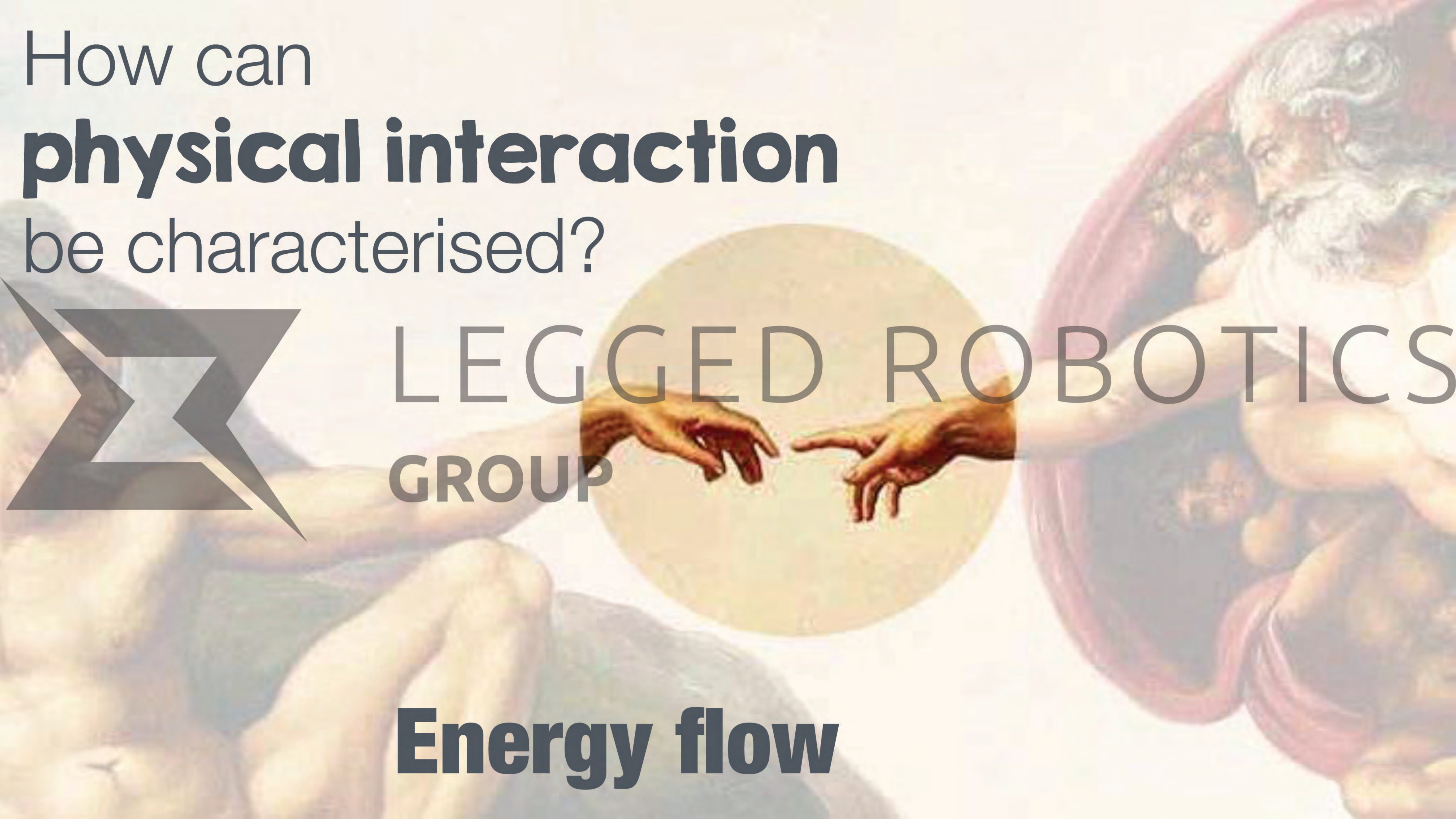


How can
physical interaction
be characterised?



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Energy flow



Ideal energetic elements



kinetic
energy



elastic
potential energy

Energy Flow

Energy Flow




Power

= energy flow

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$$P = \frac{dE}{dt}$$



$$P = \frac{dE}{dt}$$


Temporal dependency described by:

O.D.E

**Transfer
Function**

POWER

=

EFFORT

X

FLOW



Mechanic

=

FORCE

X

VELOCITY



Electric

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=

VOLTAGE

X

CURRENT



Fluid power

=

PRESSURE

X

FLOW

POWER

=

EFFORT

X

FLOW



Mechanic

=

FORCE

X

VELOCITY

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UP



Ideal mechanical elements



$$\dot{v} = \frac{1}{m} f$$

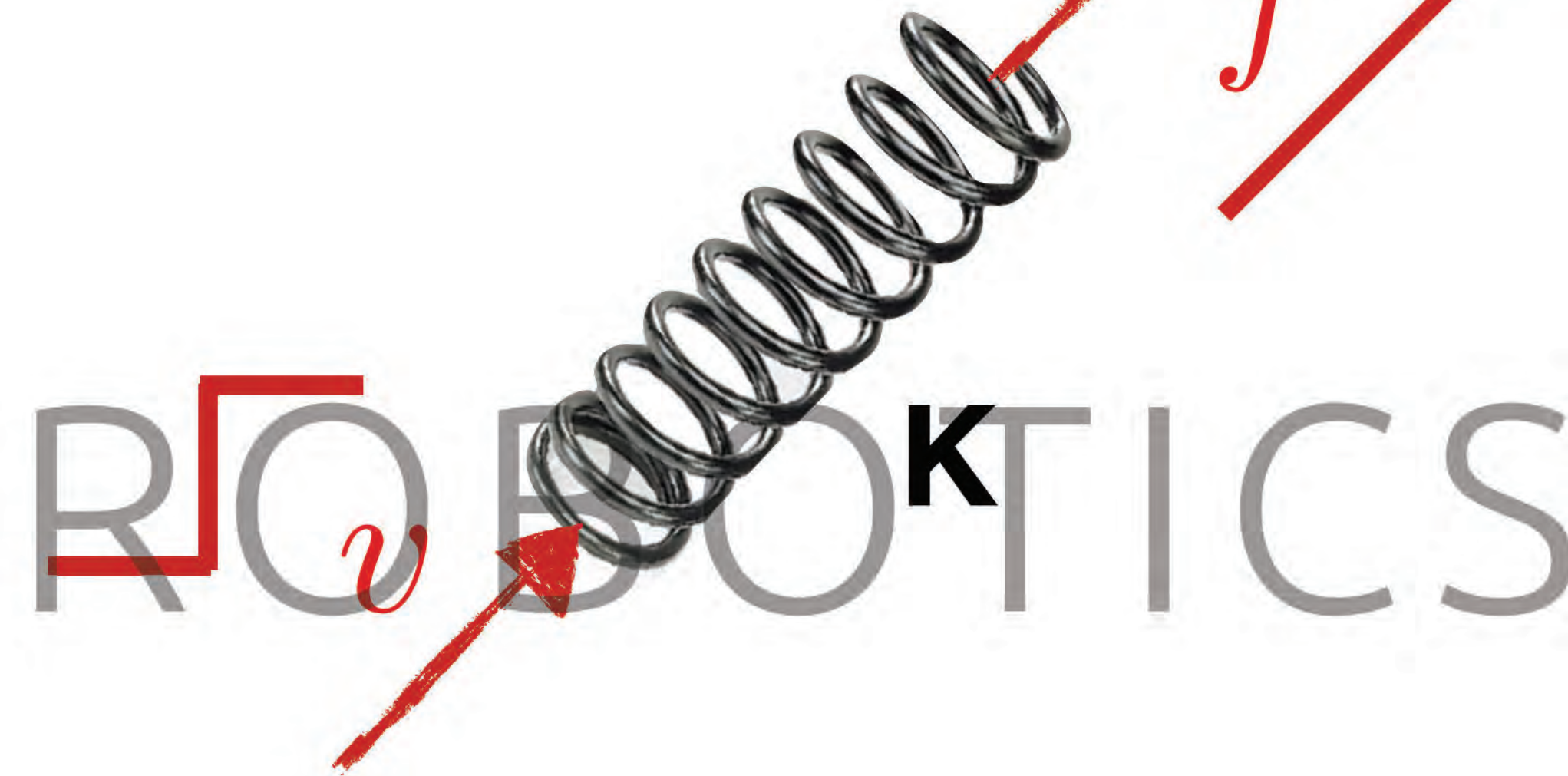
Output

v

Input

f

$$v = \int \frac{1}{m} f dt$$



$$\dot{f} = K v$$

Output

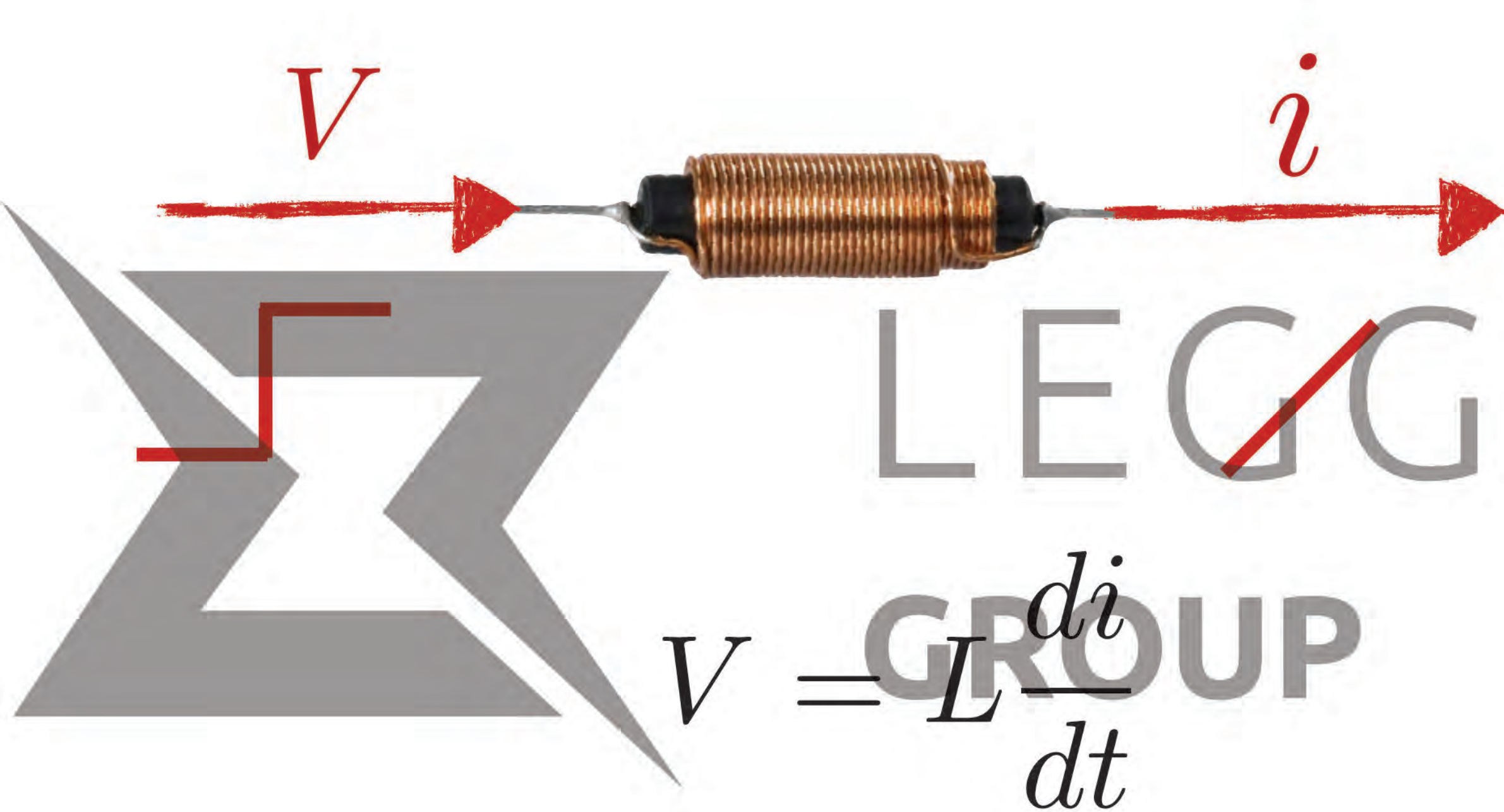
f

Input

v

$$f = \int K v dt$$

Ideal electric elements

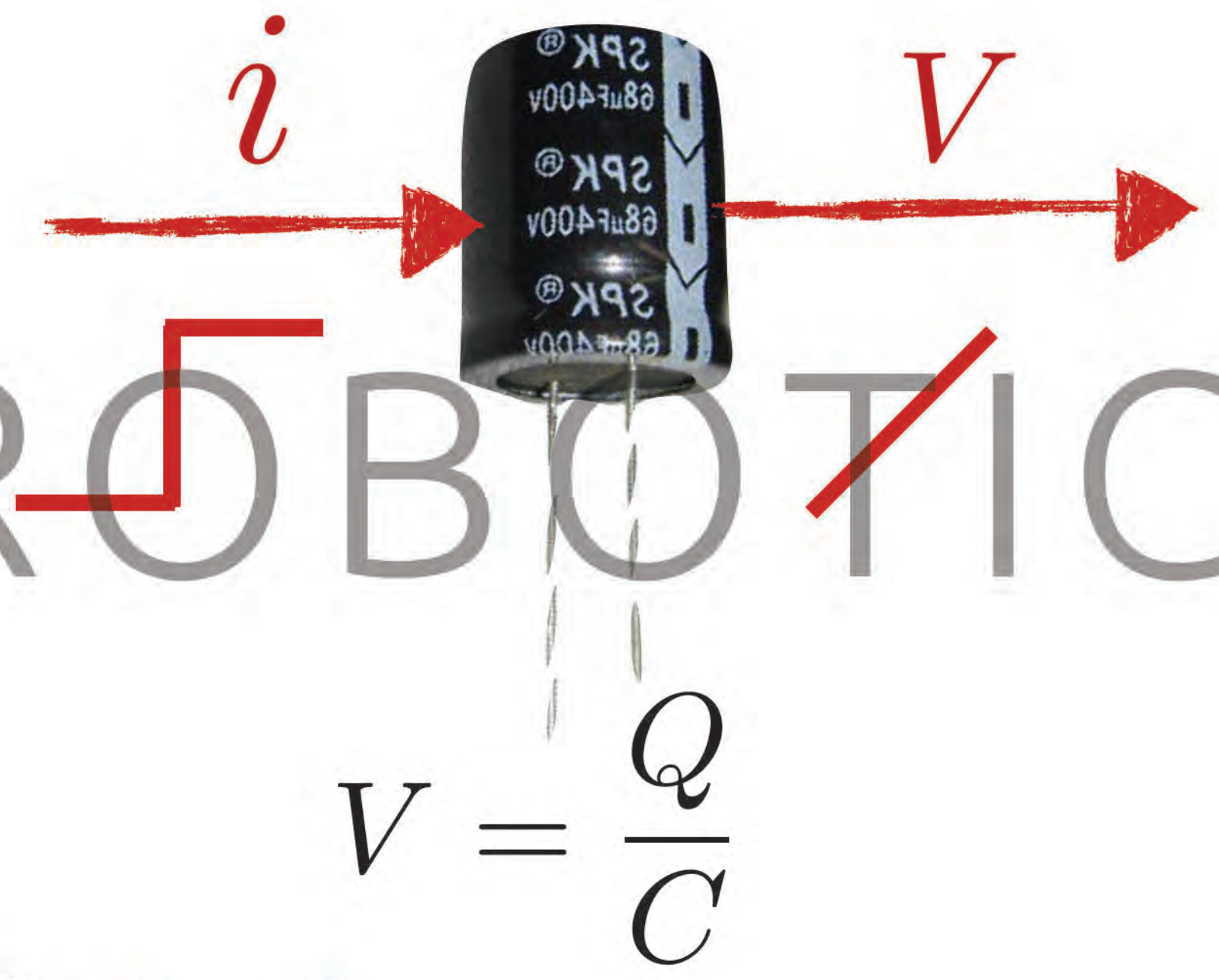


$$V = L \frac{di}{dt}$$

Output

$$i = \frac{1}{L} \int V dt$$

Input



$$V = \frac{Q}{C}$$

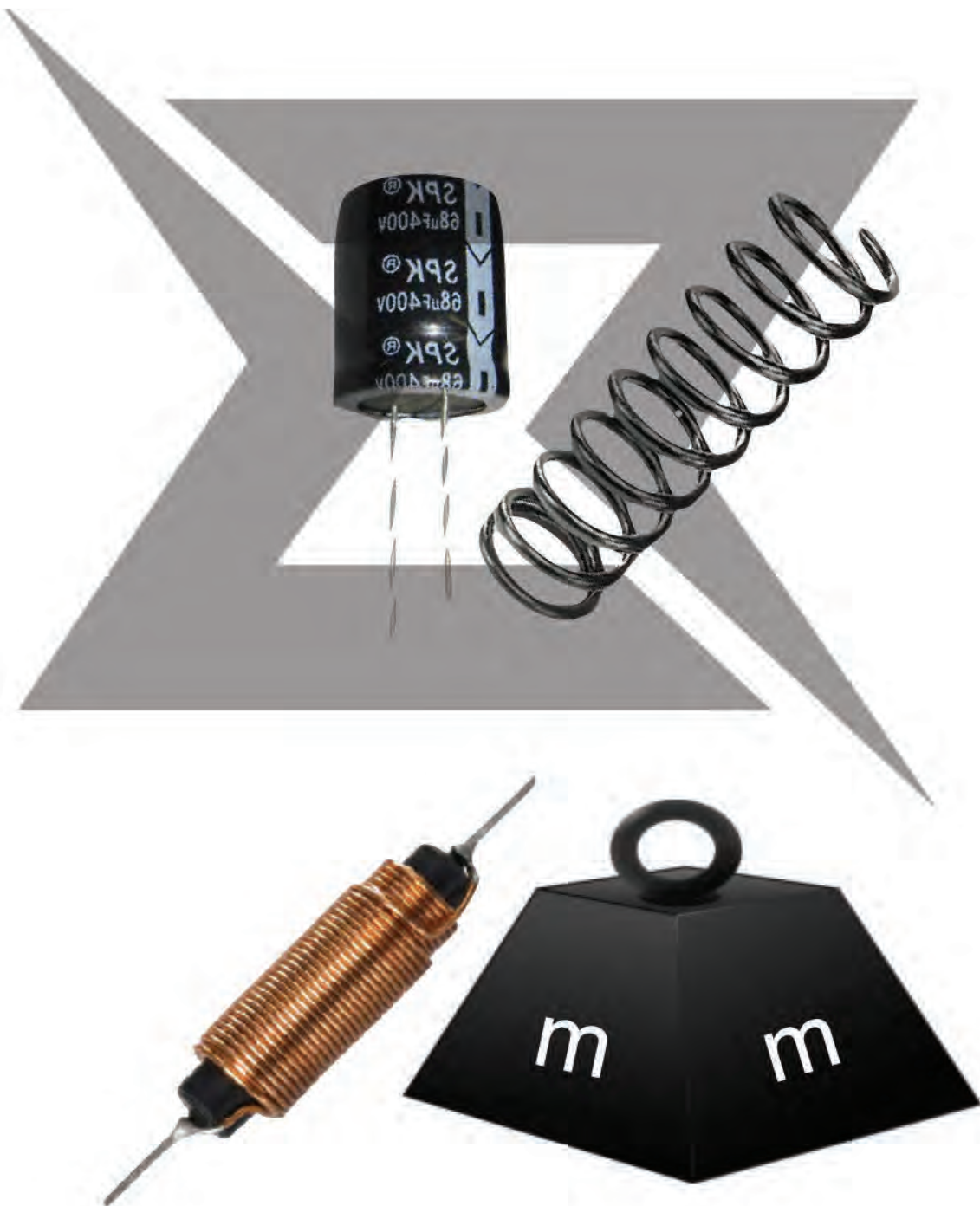
Output

$$V = \frac{1}{C} \int i dt$$

Input

Impedance and admittance

Describe a **dynamic** relation between **EFFORT/FLOW**



impedance
GROUP

INPUT
FLOW

OUTPUT
EFFORT

$$Z(s) = \frac{F(s)}{V(s)}$$

admittance

EFFORT





FLOW

$$Y(s) = \frac{V(s)}{F(s)} = \frac{1}{Z(s)}$$

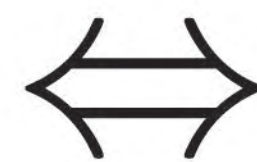
Impedance and admittance

$$Z(s) = \frac{F(s)}{V(s)}$$

$$Y(s) = \frac{V(s)}{F(s)} = \frac{1}{Z(s)}$$

Element		Impedance	Admittance
Capacitor		$Z(s) = \frac{1}{Cs}$	$Y(s) = Cs$
Inductor		$Z(s) = Ls$	$Y(s) = \frac{1}{Ls}$
Spring		$Z(s) = \frac{k}{s}$	$Y(s) = \frac{s}{k}$
Mass		$Z(s) = ms$	$Y(s) = \frac{1}{ms}$

Input/Output



Causality

Impedance Control: An Approach to Manipulation:

Part I—Theory

The most important consequence of dynamic interaction between two physical systems is that one must physically complement the other: Along any degree of freedom, if one is an impedance, the other must be an admittance and vice versa. Now, for almost all manipulatory tasks the environment at least contains inertias and/or kinematic constraints, physical systems which accept force inputs and which determine their own motion in response. However, as described above, while a constrained inertial object can always be pushed on, it cannot always be moved; These systems are properly described as admittances. Seen from the manipulator, the world is an admittance.

[Hogan, 1985]

Inertia



minimum model for most **objects**



prefer causality of **admittance**

Kinematic constraint

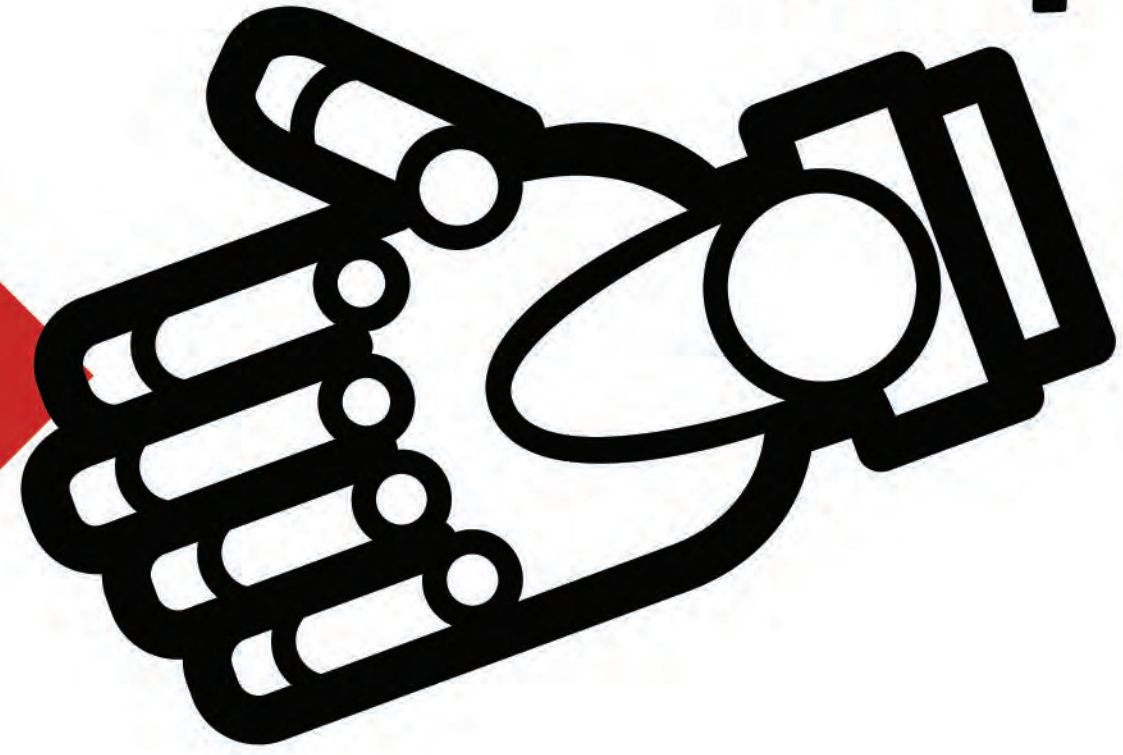
$$\dot{x} = \ddot{x} = 0$$

simplest description of **contacts**



require causality of **admittance**

impedance



admittance

impedance



admittance

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During

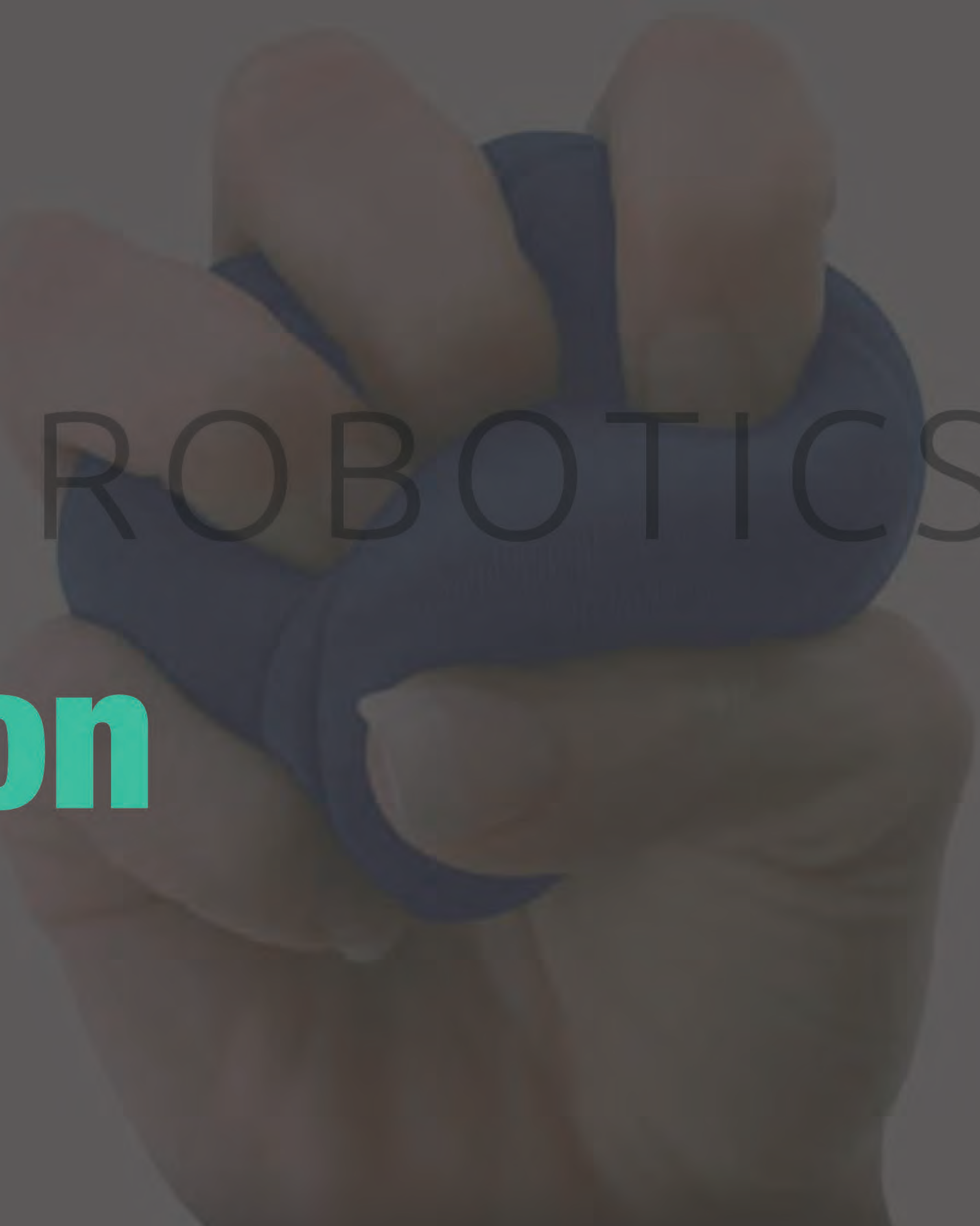
physical interaction,

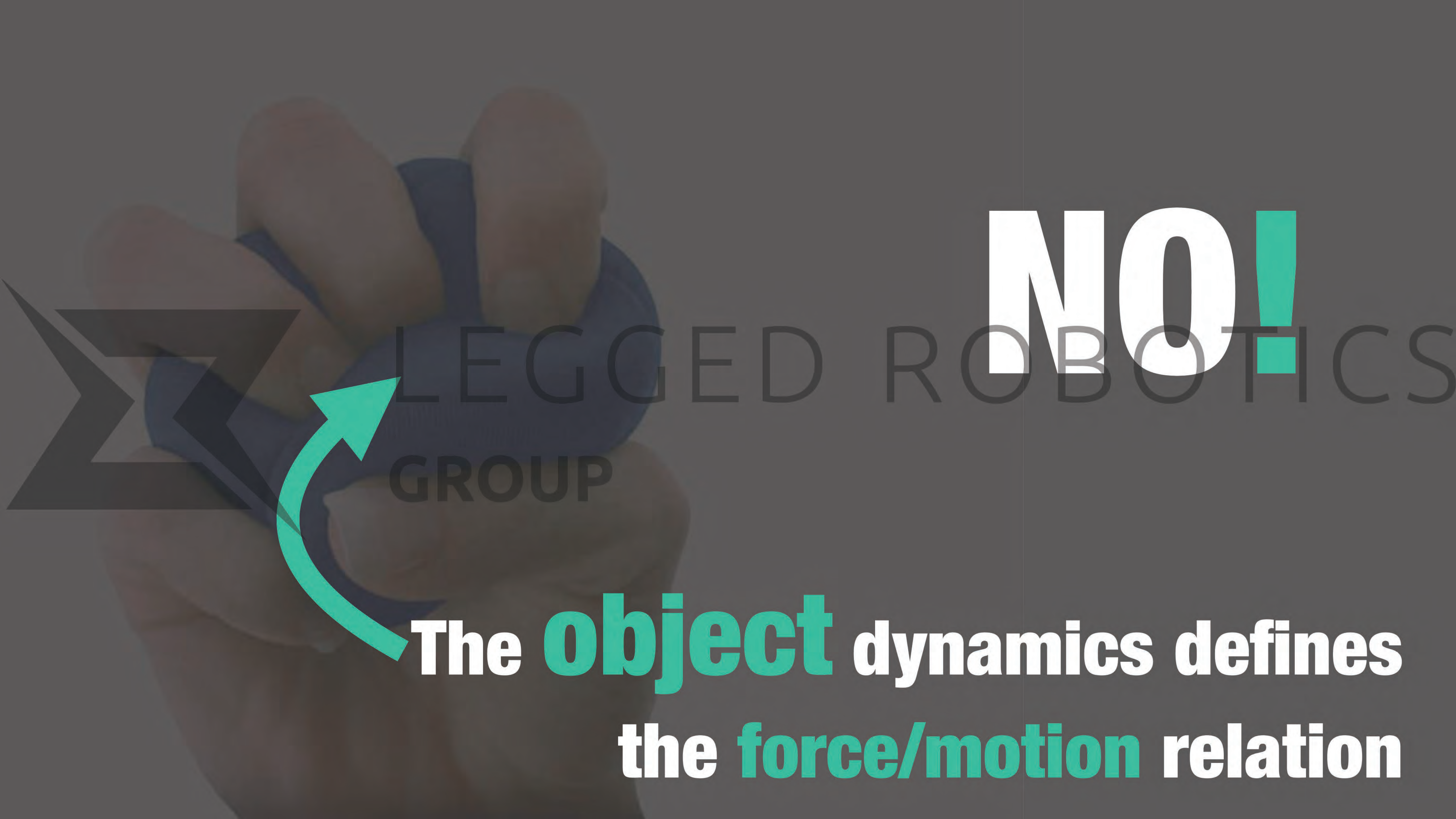
can we control

force and position

independently?

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NO!

The **object** dynamics defines
the **force/motion** relation

**não é afetado pelo
contato e interação**

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Alternative:

**To control the
dynamic behaviour
of the interaction points**

Alternative:

To control the

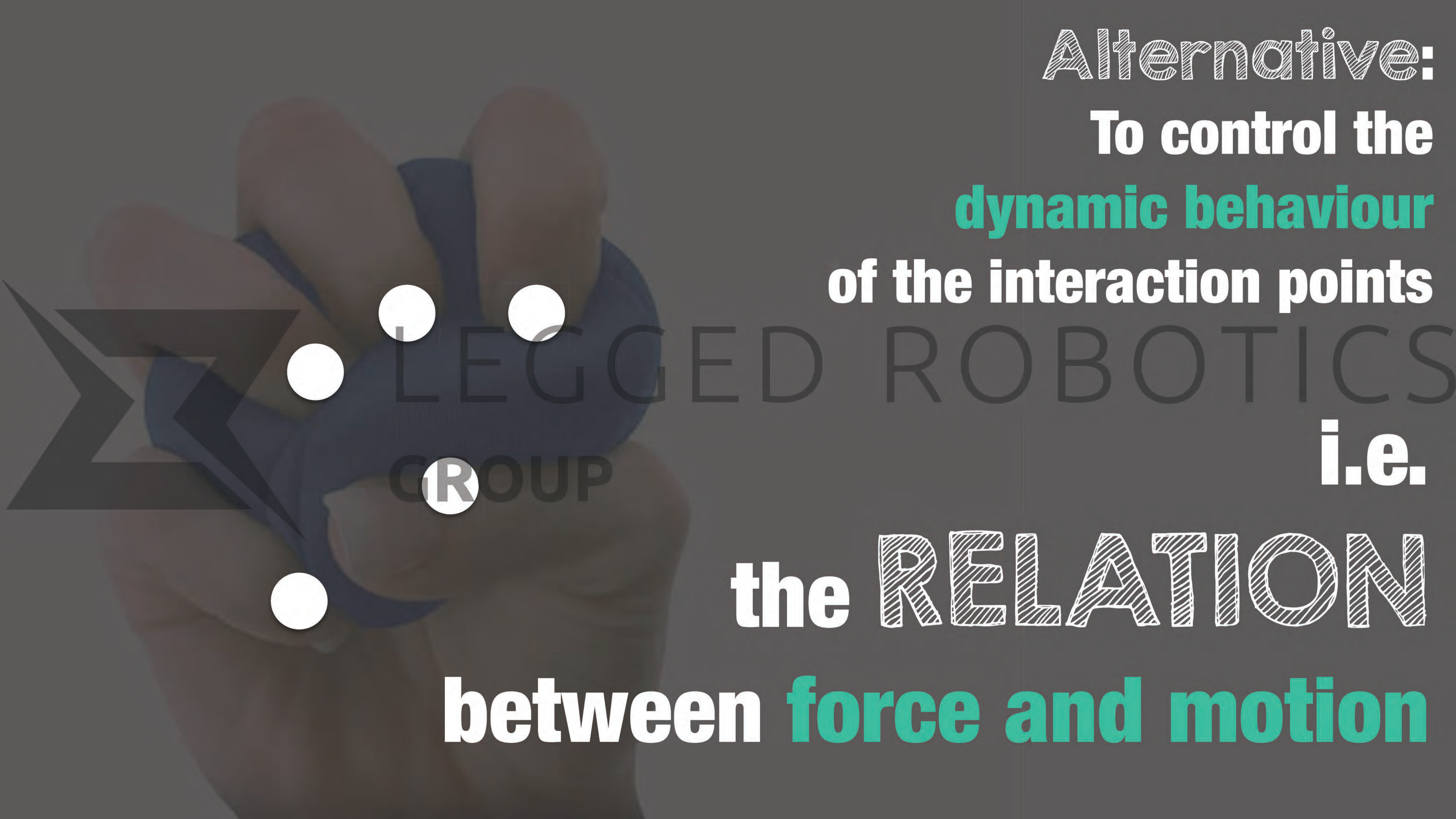
dynamic behaviour

of the interaction points

i.e.

the **RELATION**

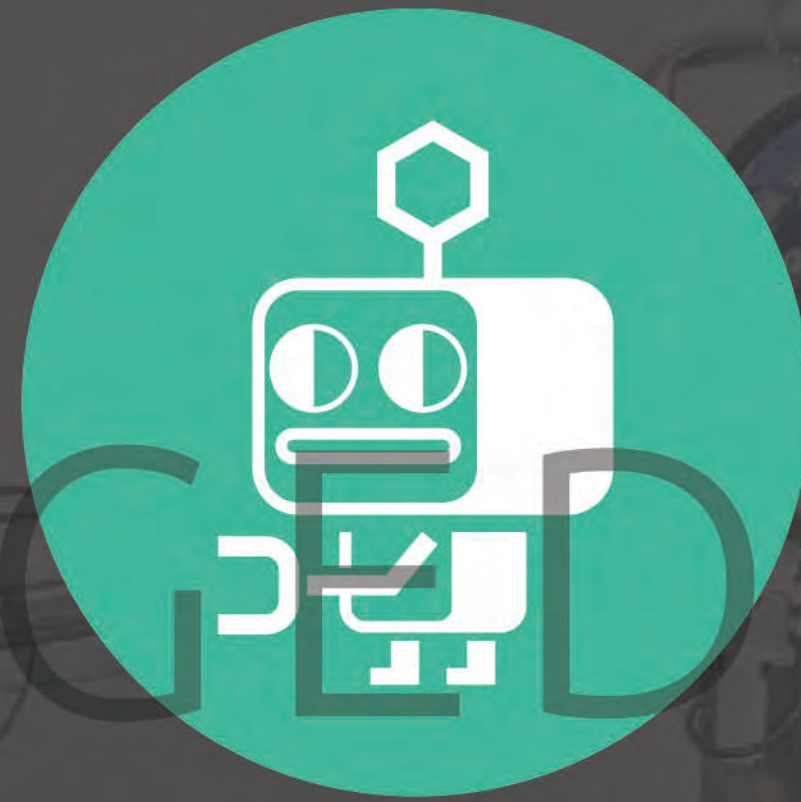
between **force and motion**



interaction control



basic
principle



impedance
control

Impedance Control

Establish a **dynamic relation** between **force** and **position**

$$F = M\ddot{x} + B\dot{x} + Kx$$

Inertia

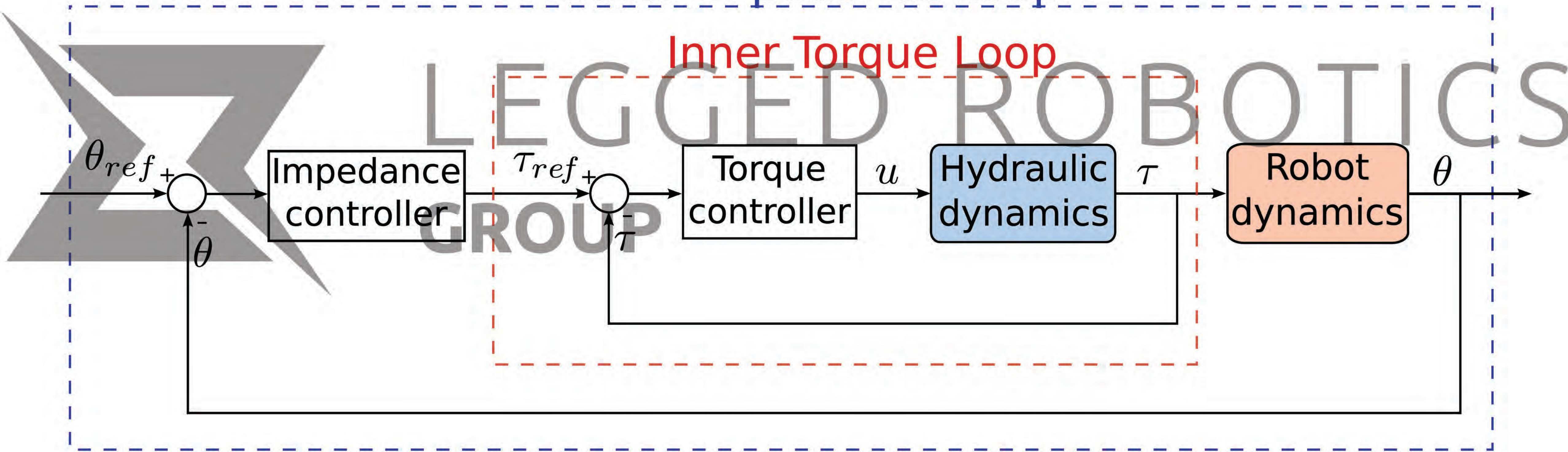
Damping

Stiffness

Classic Architecture

Outer Impedance Loop

Inner Torque Loop



Mimicking
passive leg



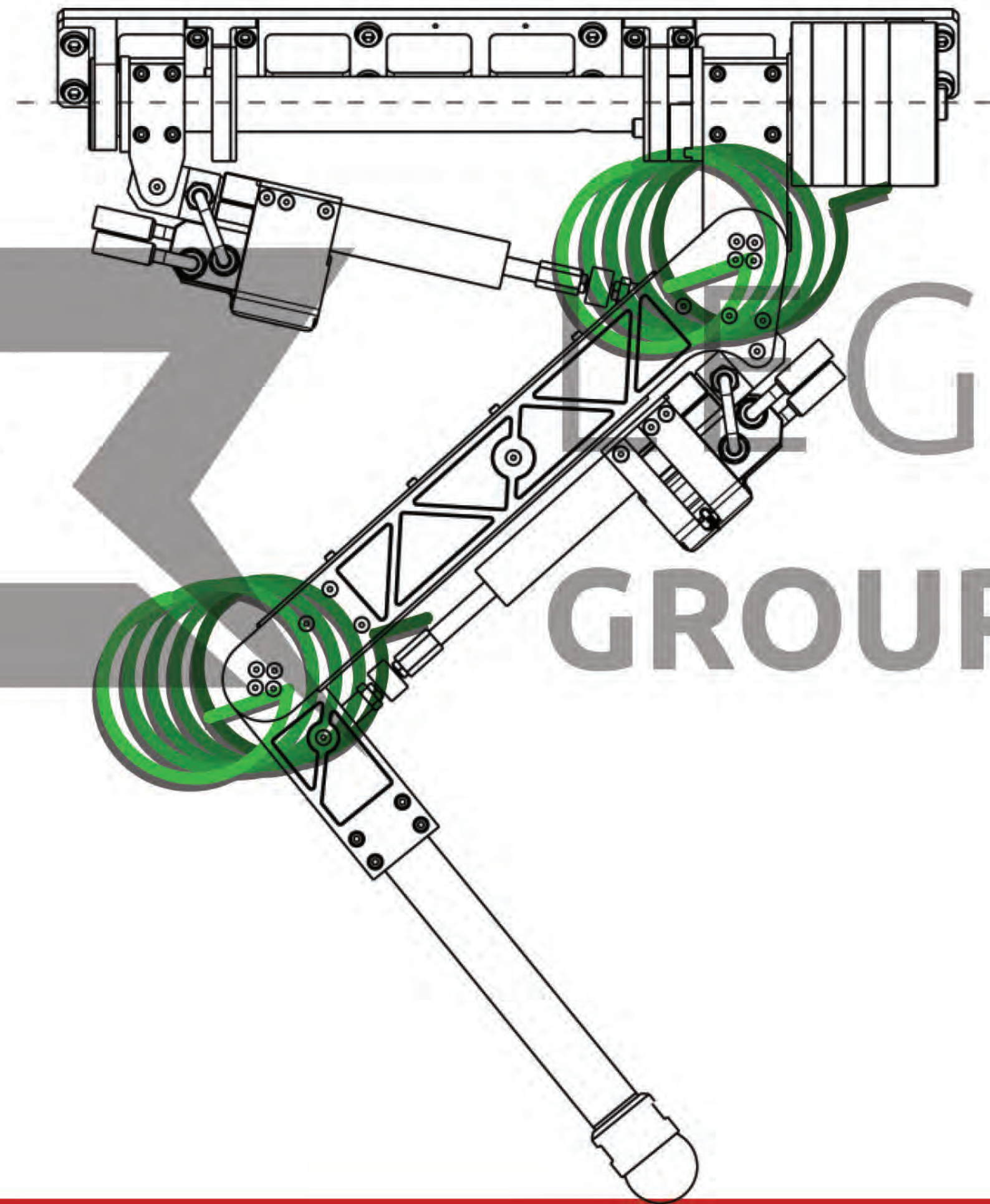
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$$\tau = K\theta + B\dot{\theta}$$

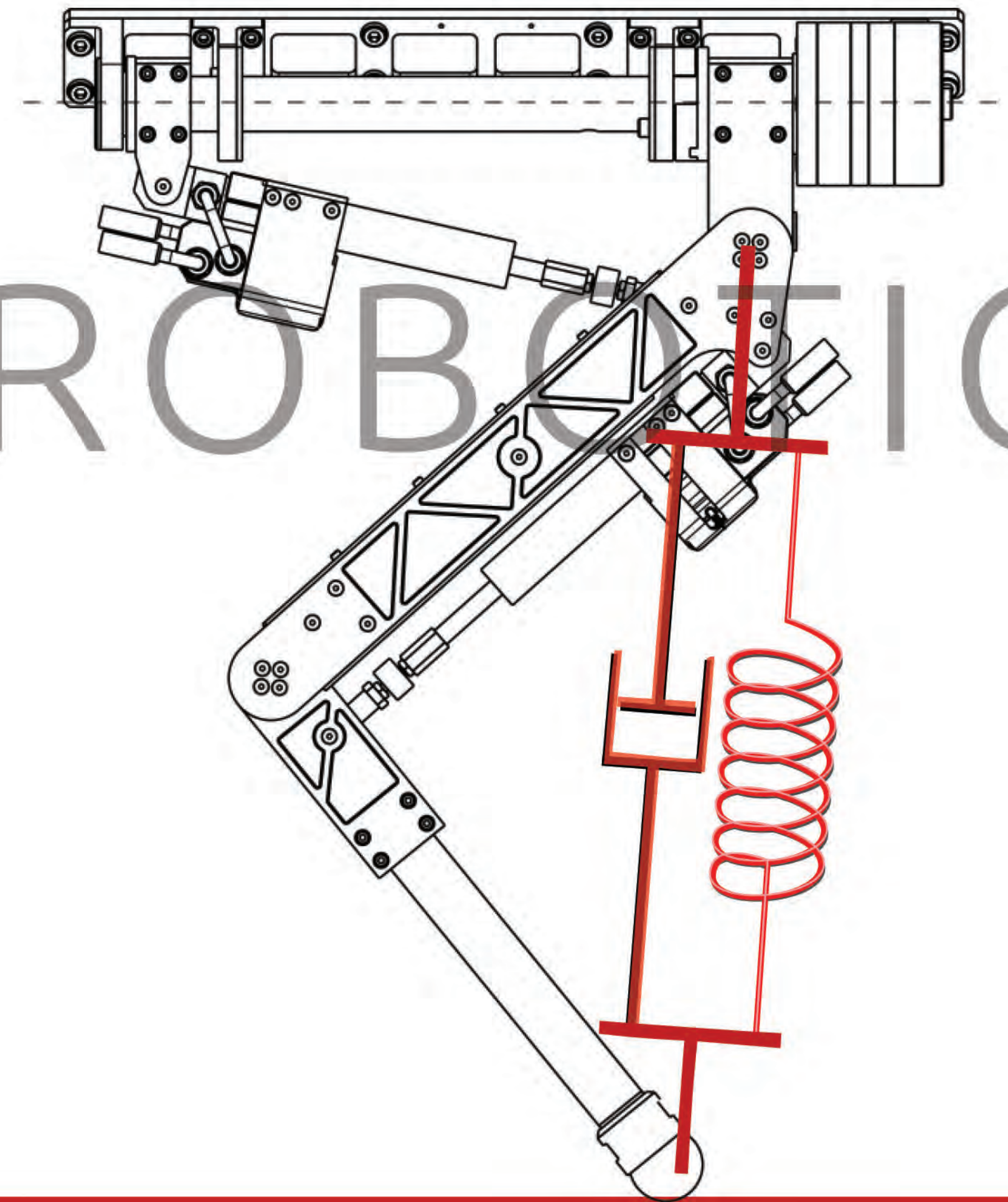
Joint space



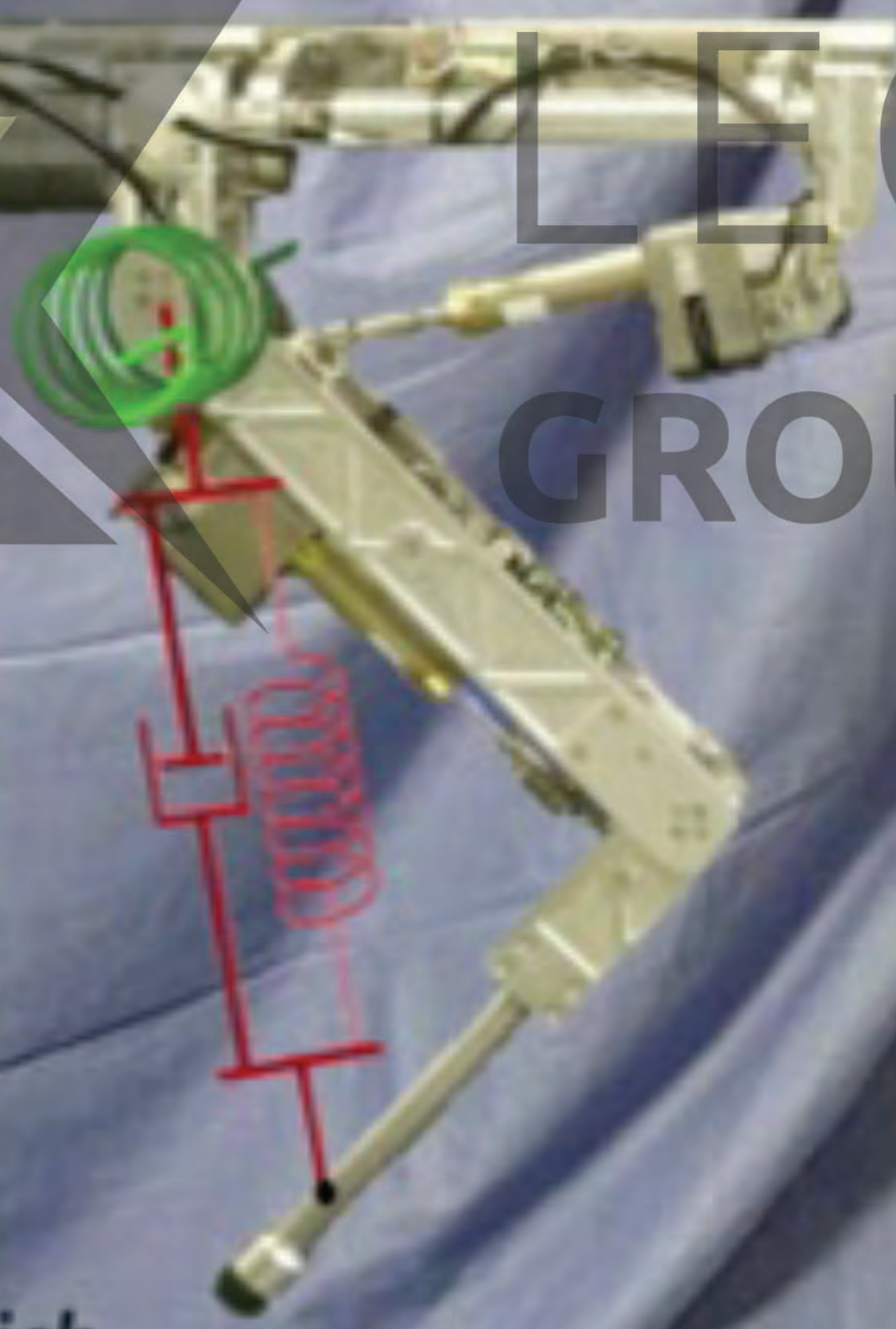
Joint space vs. Task space



vs.

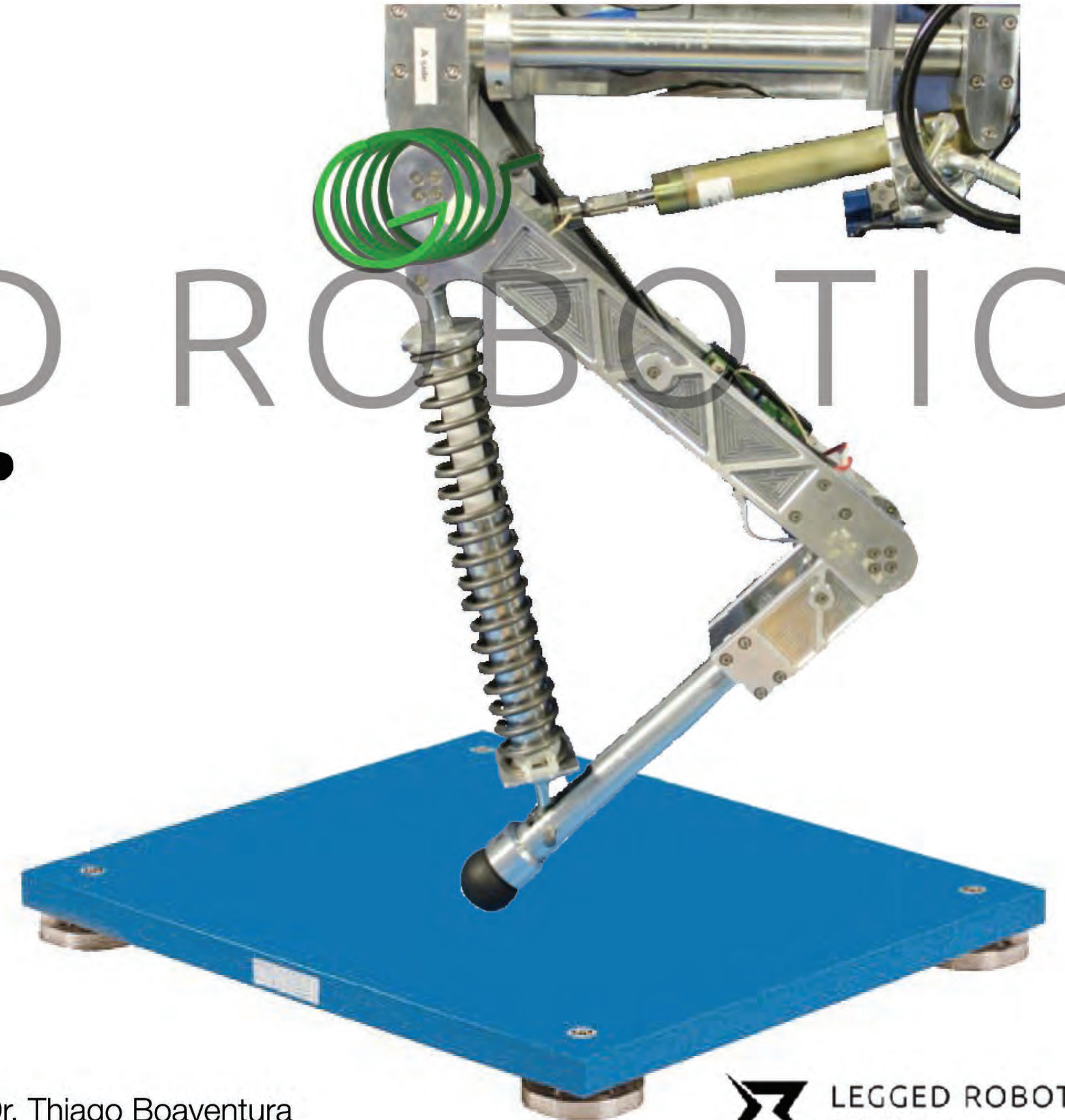
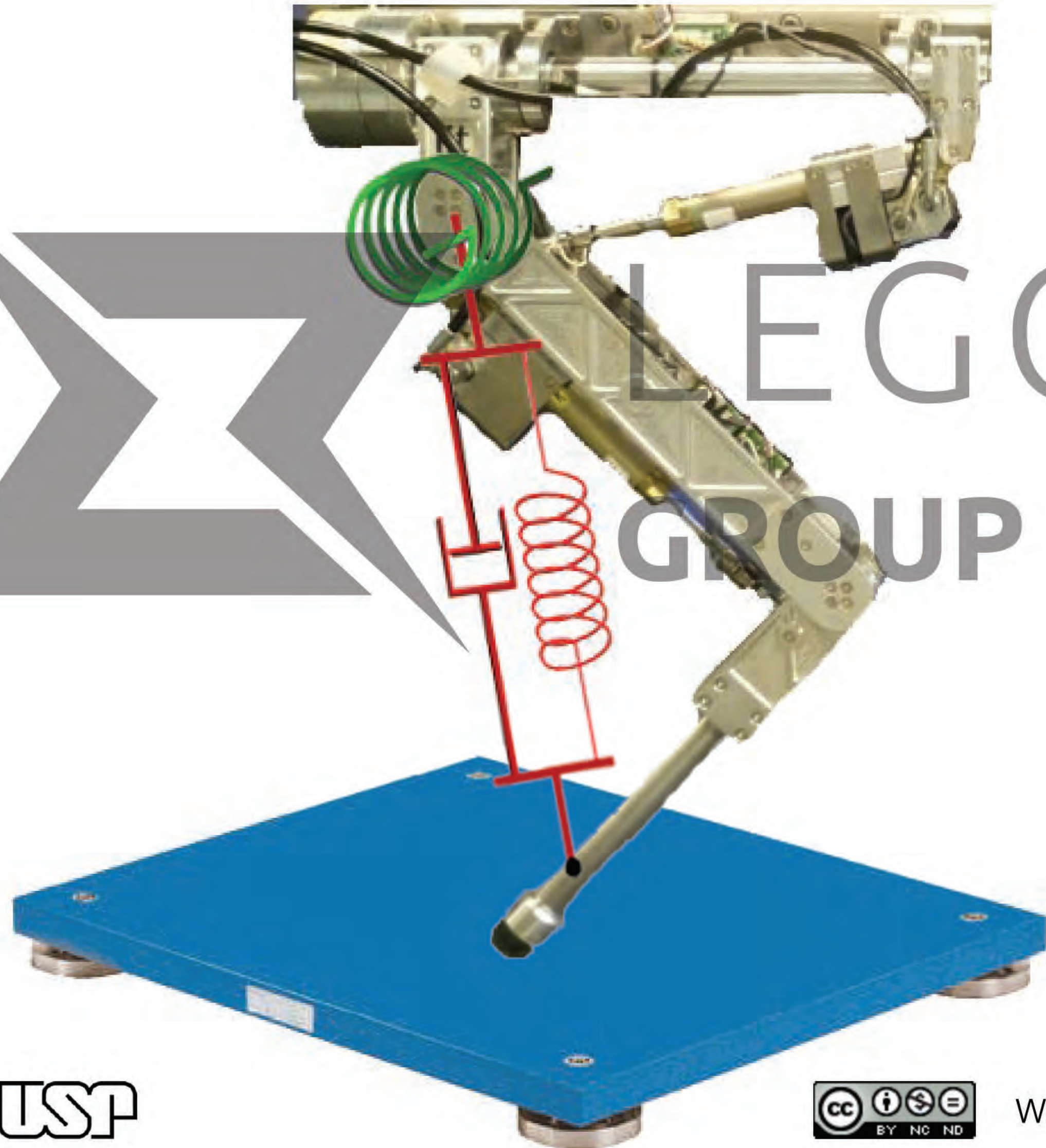


Virtual springs:
Rotational spring at hip
Linear spring in leg



Active impedance (task space)

Passive impedance

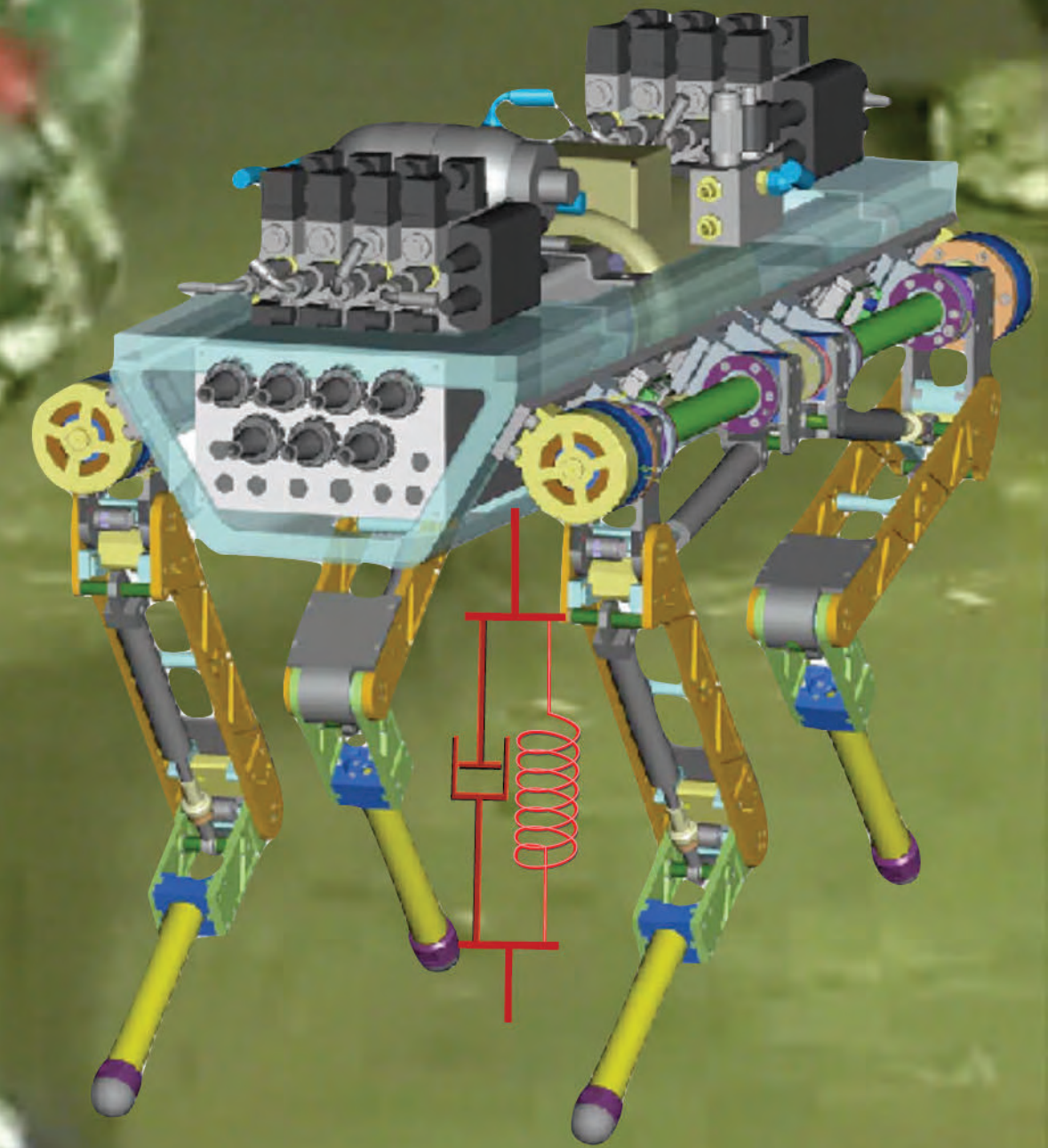


vs.

Active Impedance vs. Passive Impedance

Drop test – Speed 1/16

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Approaches to control the robot impedance



joint
control

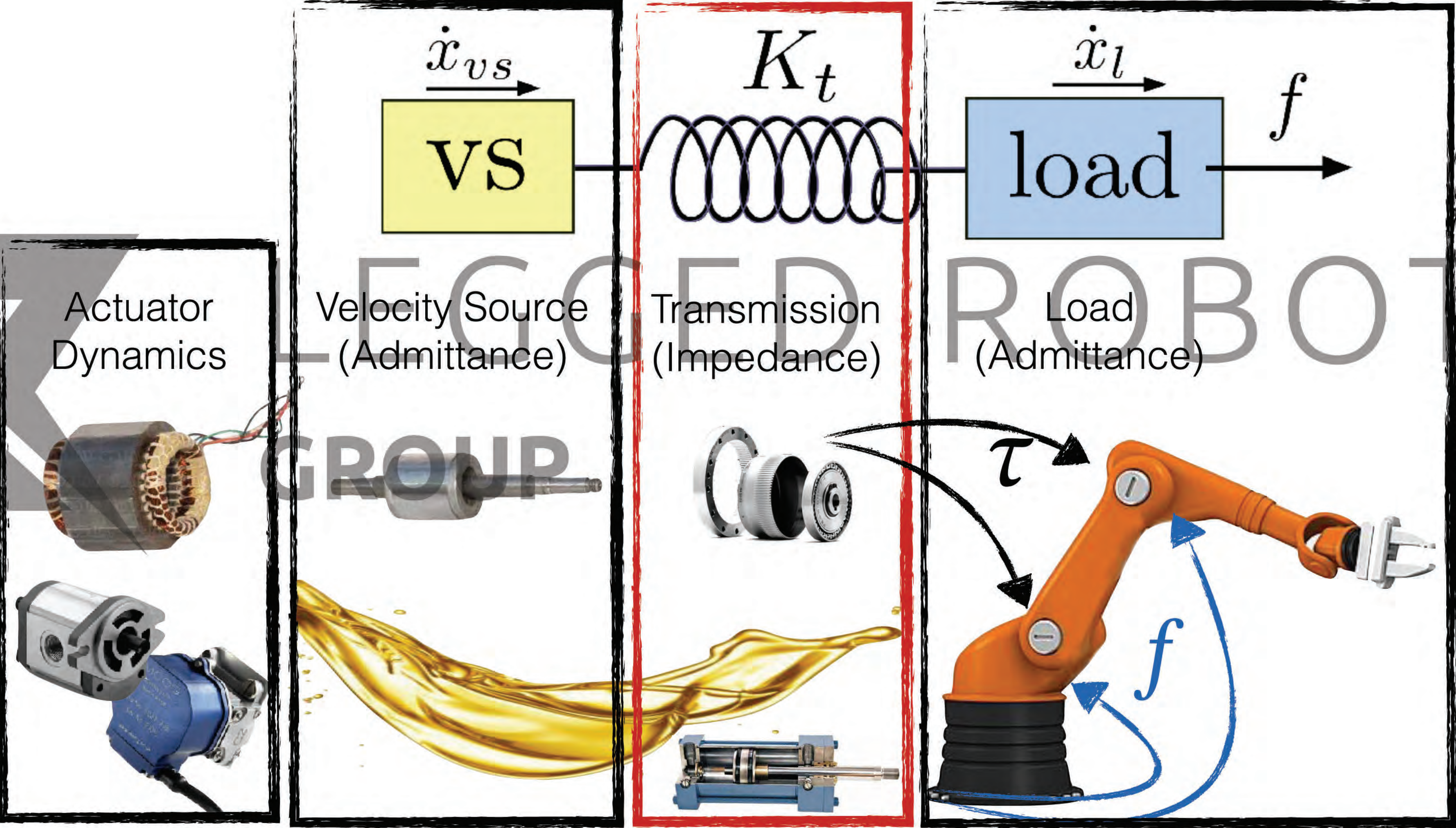


kinematic
configuration



contact
points

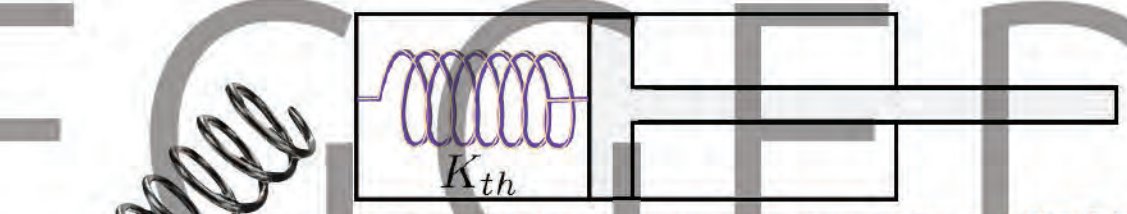
Actuation Chain



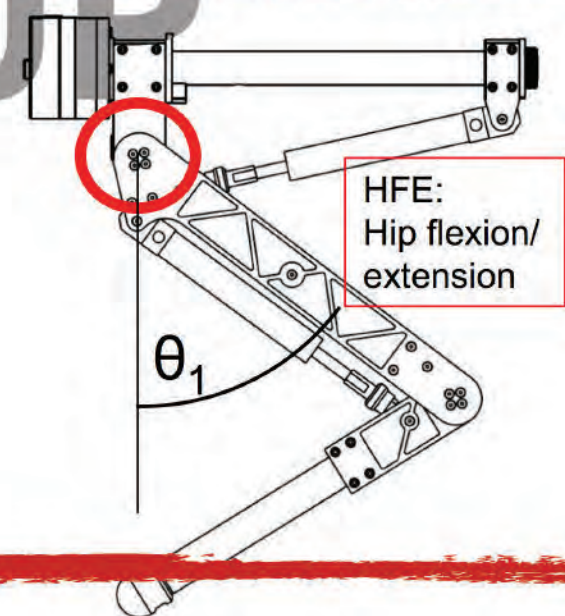
Transmission stiffness



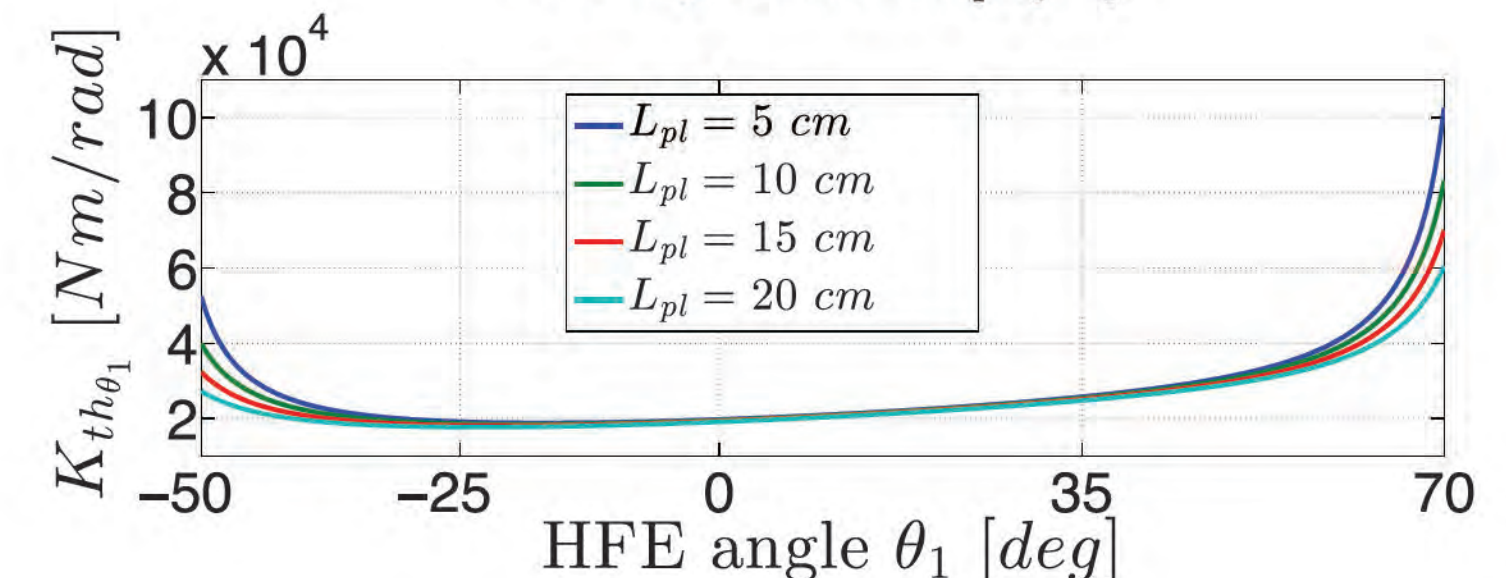
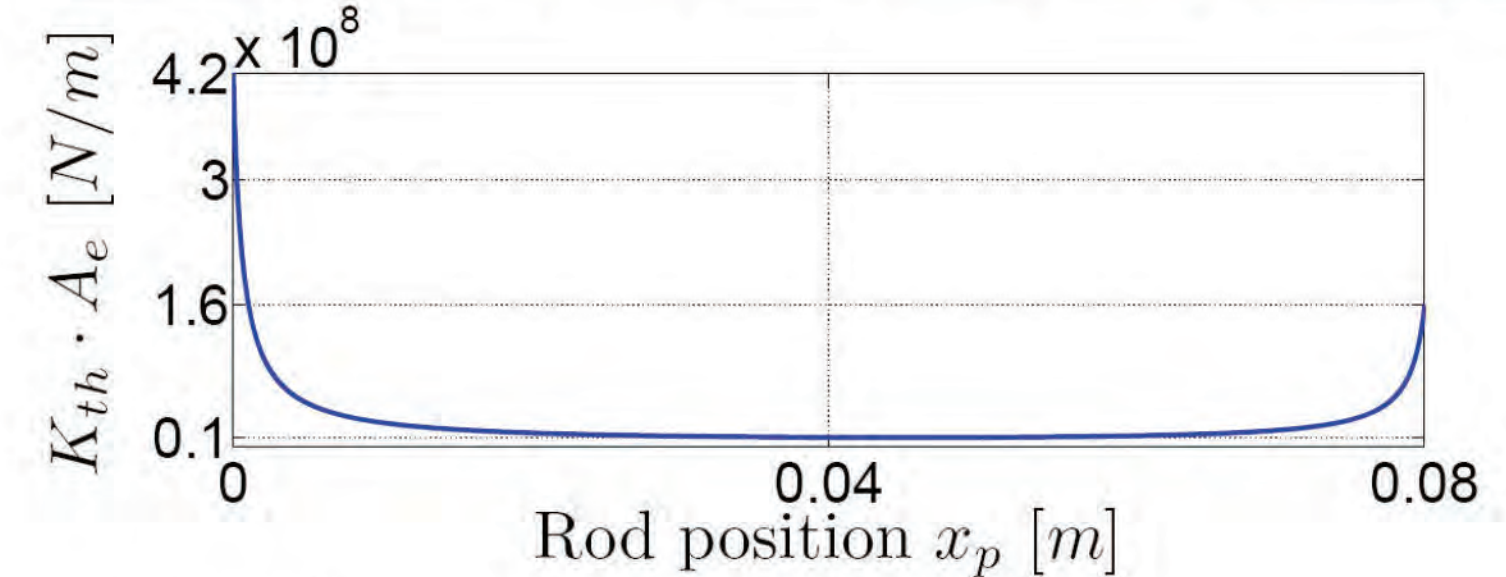
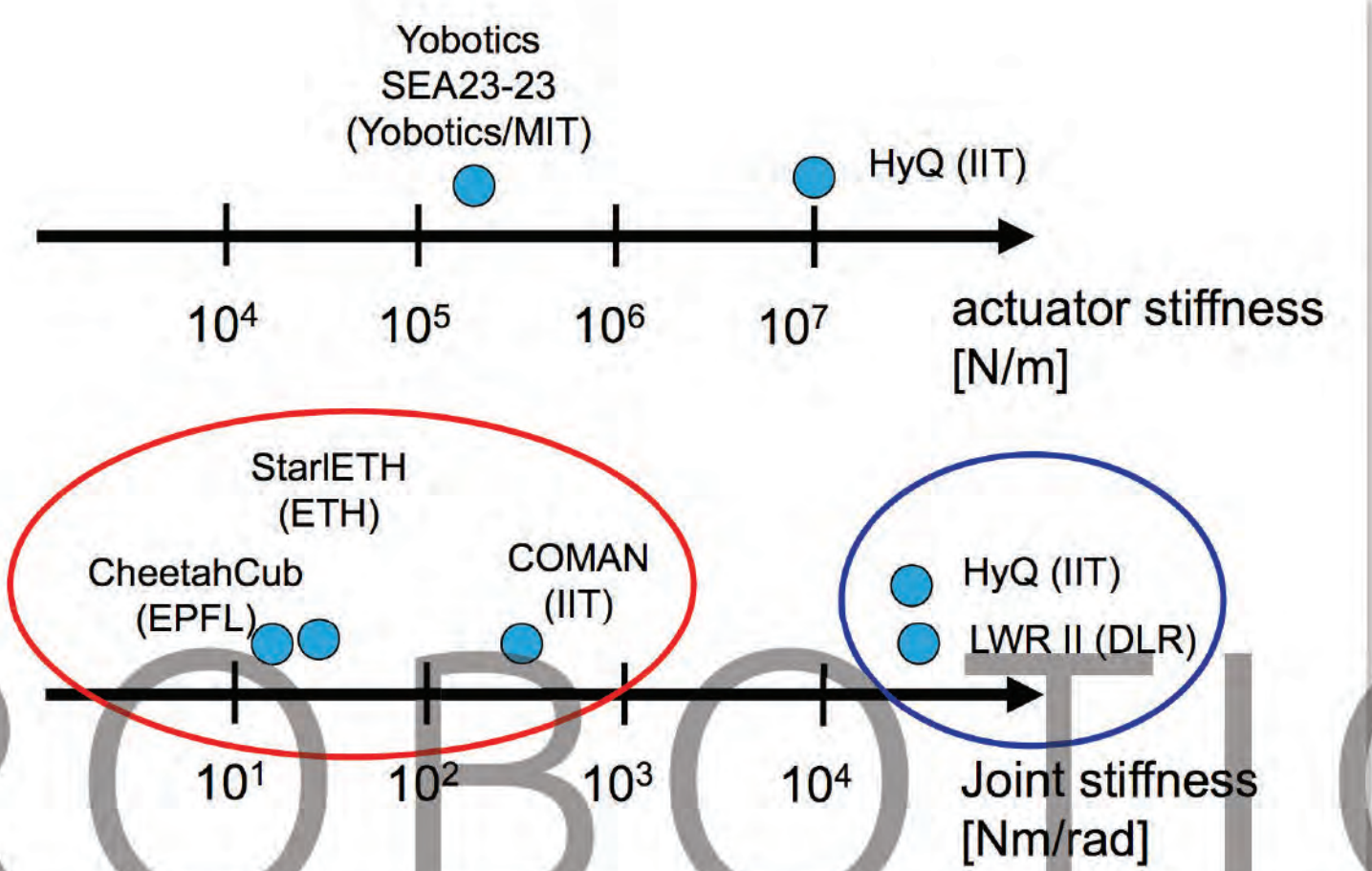
$2.7 \times 10^4 \text{ Nm/rad}$



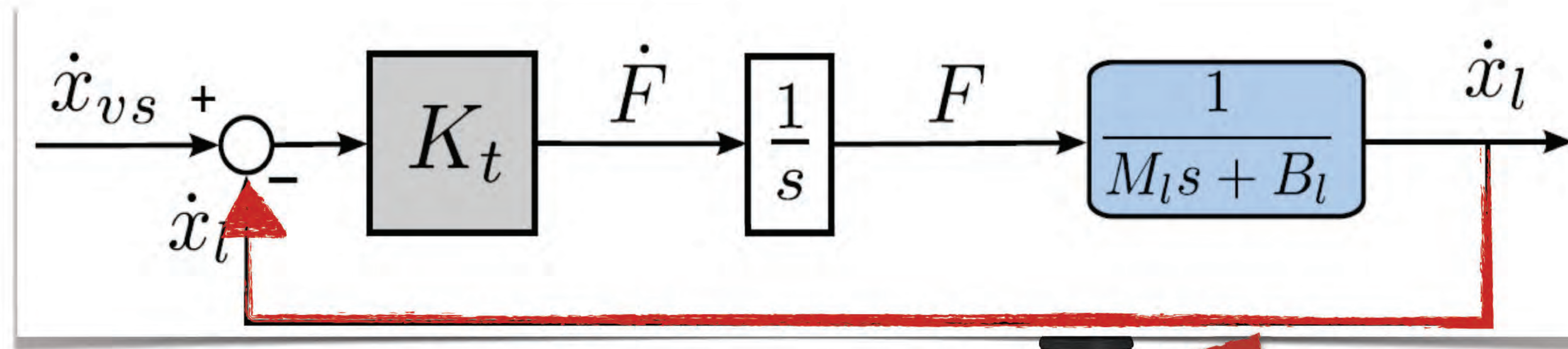
$0.9 \times 10^7 \text{ N/m}$



$2.1 \times 10^4 \text{ Nm/rad}$



Intrinsic Velocity Feedback



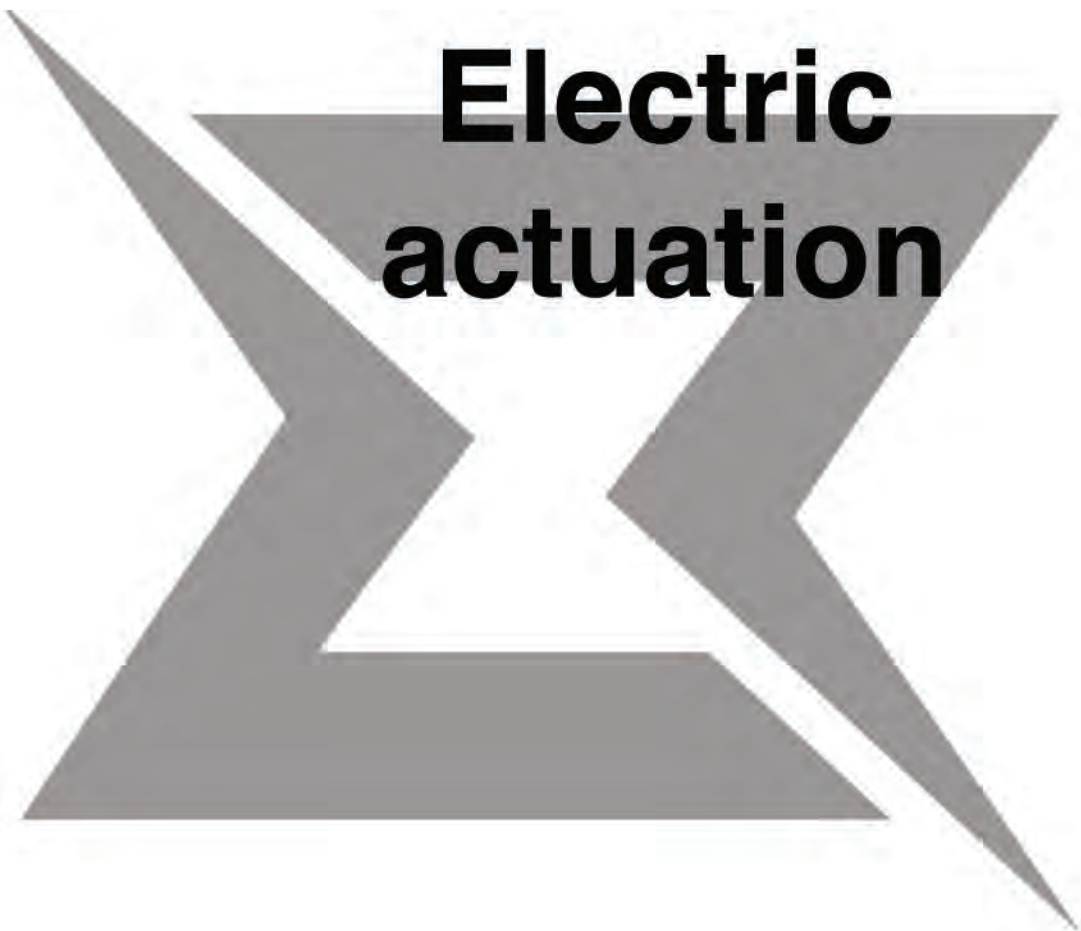
**Natural velocity feedback:
it does not depend on
the actuation system!**

$$f = K_t (\dot{x}_{vs} - \dot{x}_l)$$

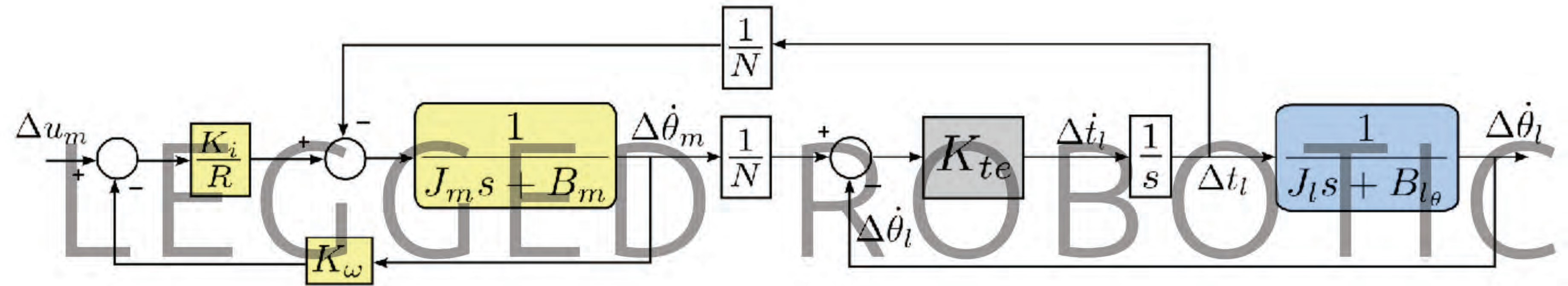
Boaventura, T., et al. On the role of load motion compensation in high-performance force control. IROS, 2012

Intrinsic Velocity Feedback

Open-loop torque/force dynamics

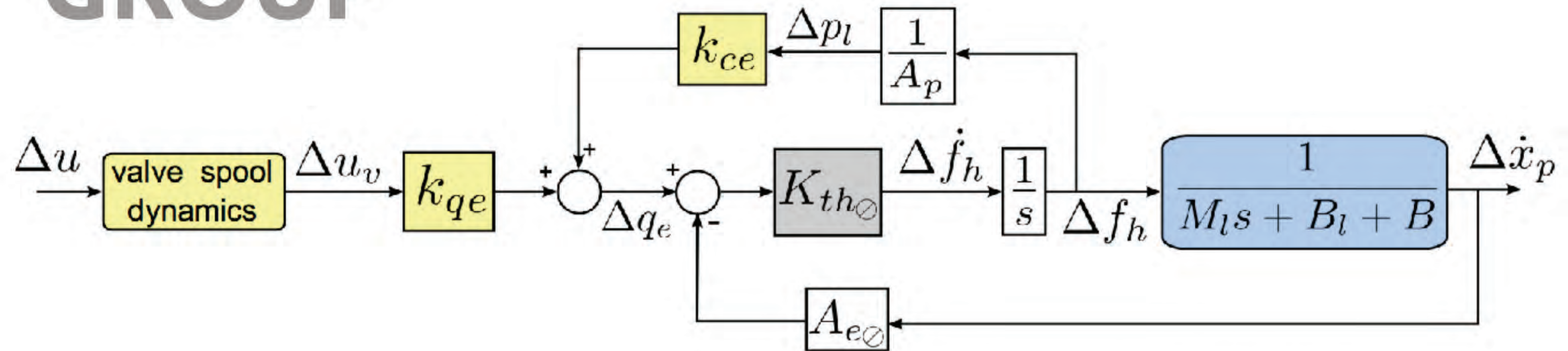


Electric
actuation



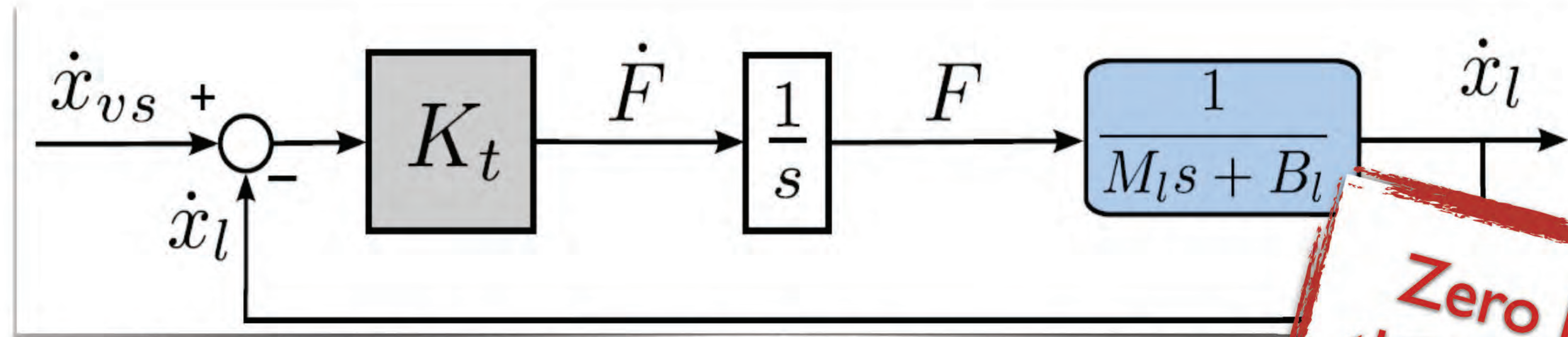
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Hydraulic
actuation



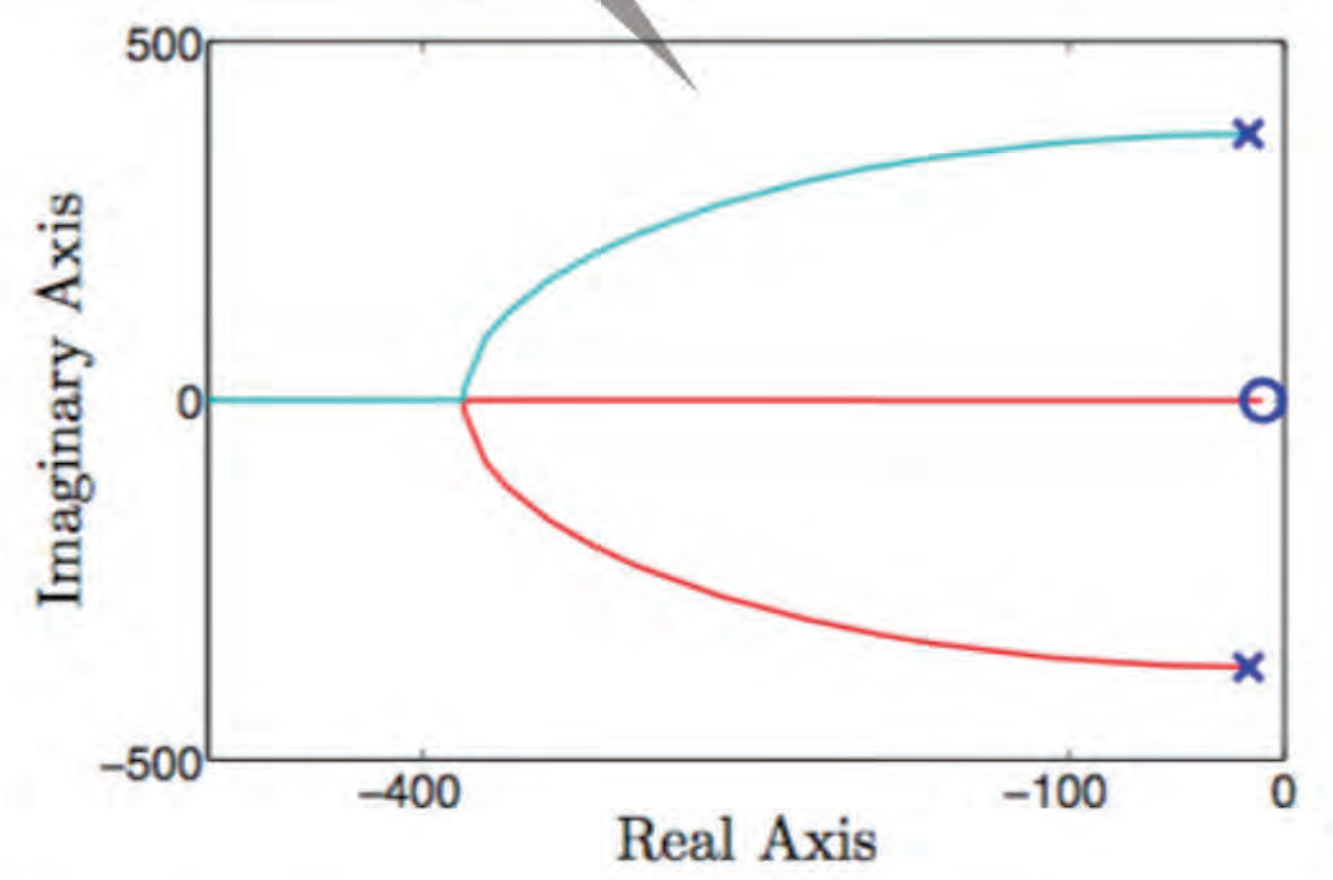
Boaventura, T., et al. On the role of load motion compensation in high-performance force control. IROS, 2012

Intrinsic Velocity Feedback



Zero limits the response.

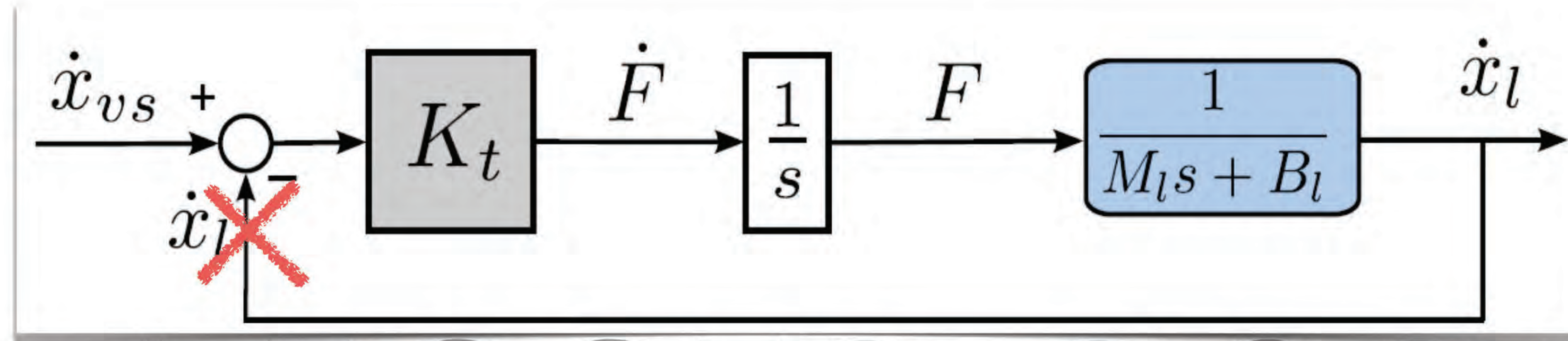
$$\frac{f(s)}{\dot{x}_{vs}(s)} = \frac{K_t (M_l s + B_l)}{s (M_l s + B_l) + K_t}$$



It does not depend on the actuation

Use of load motion compensation in high-performance force control. IROS, 2012

Model-based velocity compensation



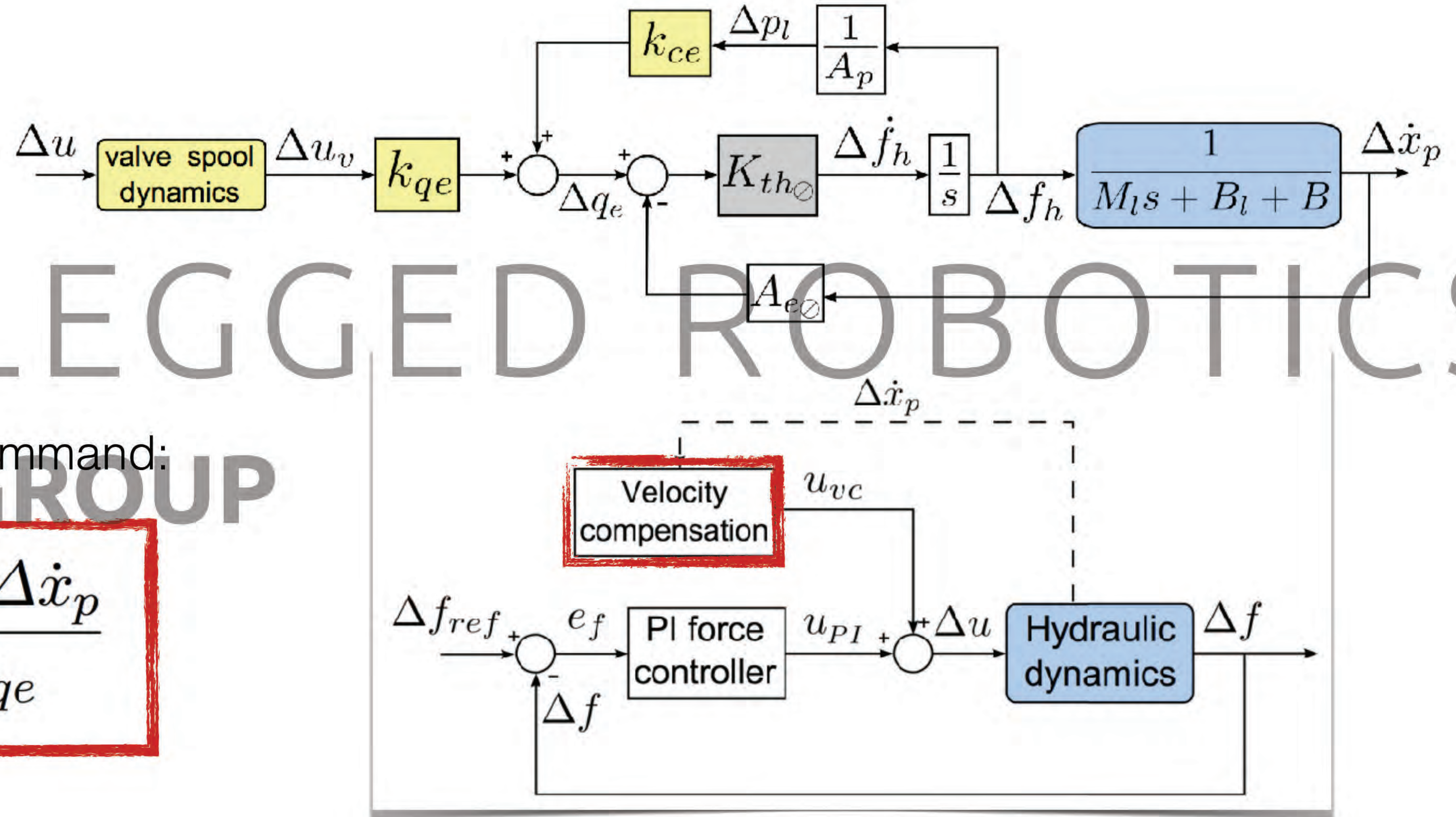
$$\frac{f(s)}{\dot{x}_{vs}(s)} = \frac{K_t (M_l s + B_l)}{s (M_l s + B_l) + \cancel{K_t}} = \frac{K_t}{s}$$

$$\dot{x}_{ex} = \dot{x}_l$$

Boaventura, T., et al. On the role of load motion compensation in high-performance force control. IROS, 2012

Model-based velocity compensation

Hydraulic
actuation

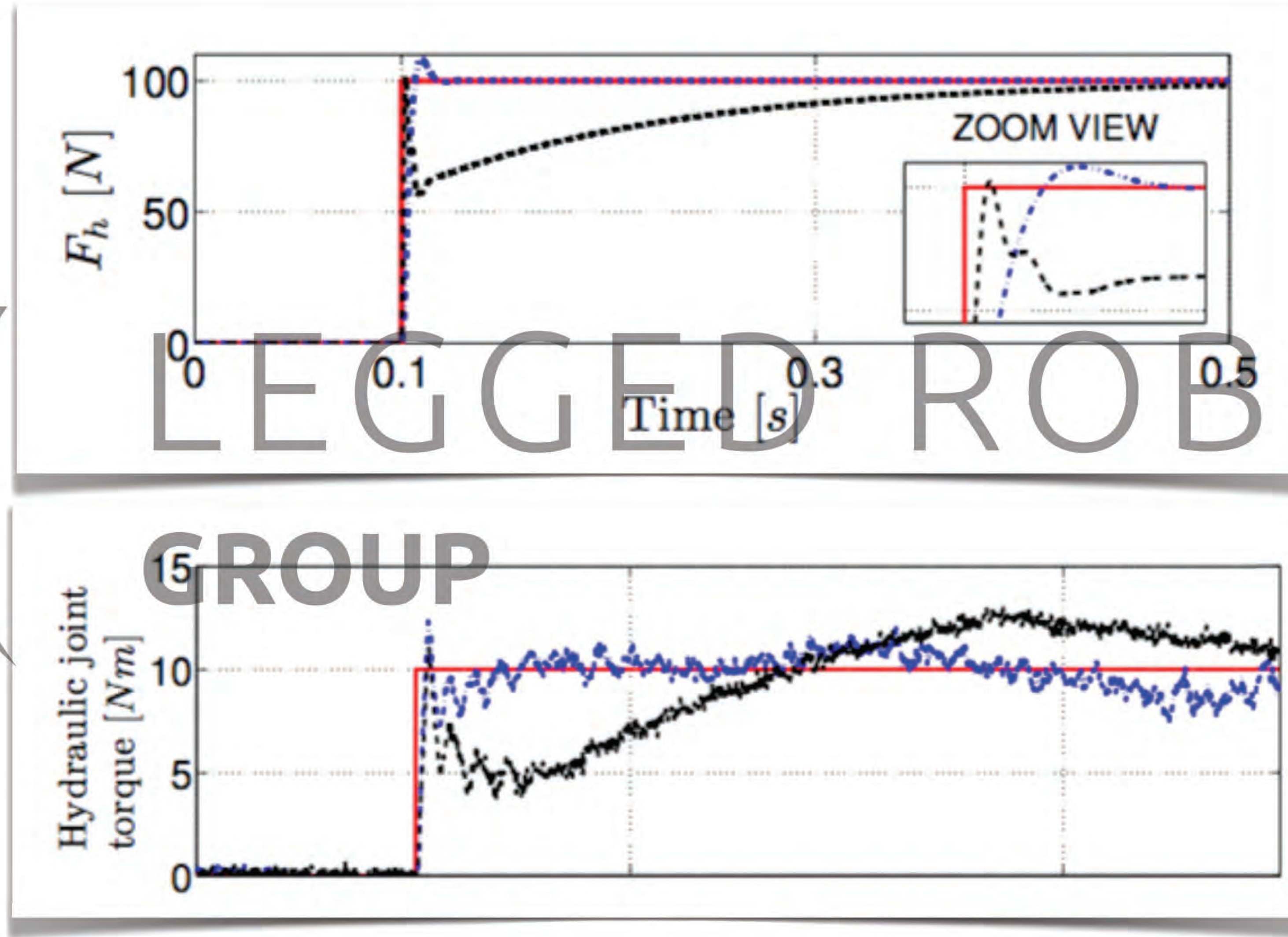


Feedforward command:

$$u_{vc} = \frac{A_{e\phi} \Delta \dot{x}_p}{K_{qe}}$$

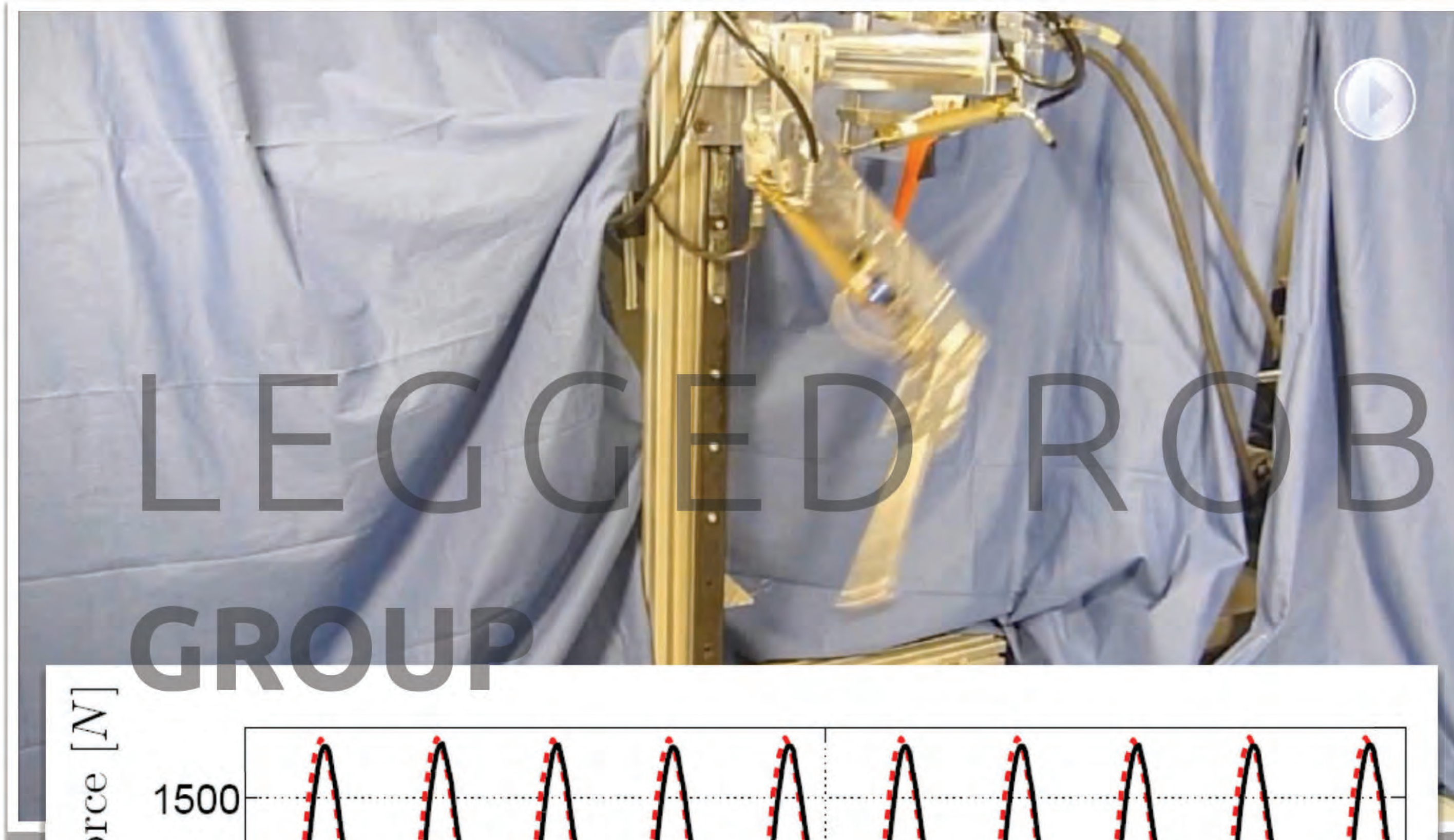
Boaventura, T., et al. On the role of load motion compensation in high-performance force control. IROS, 2012

Model-based velocity compensation

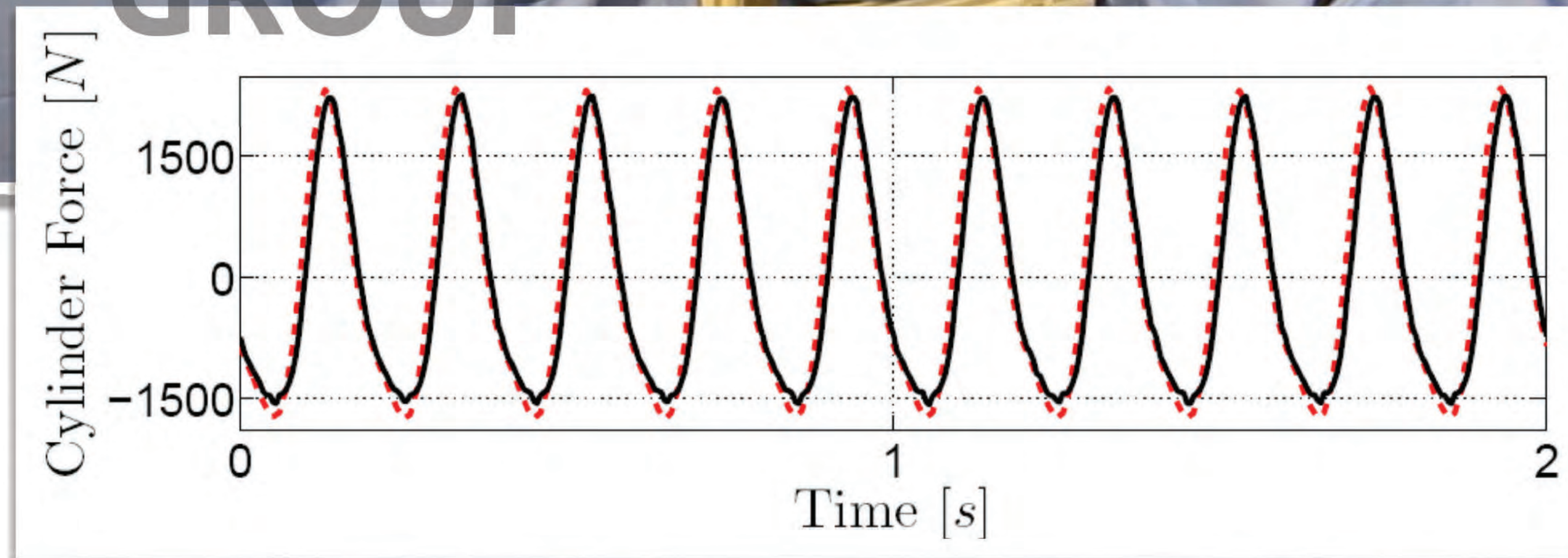


Boaventura, T., et al. On the role of load motion compensation in high-performance force control. IROS, 2012

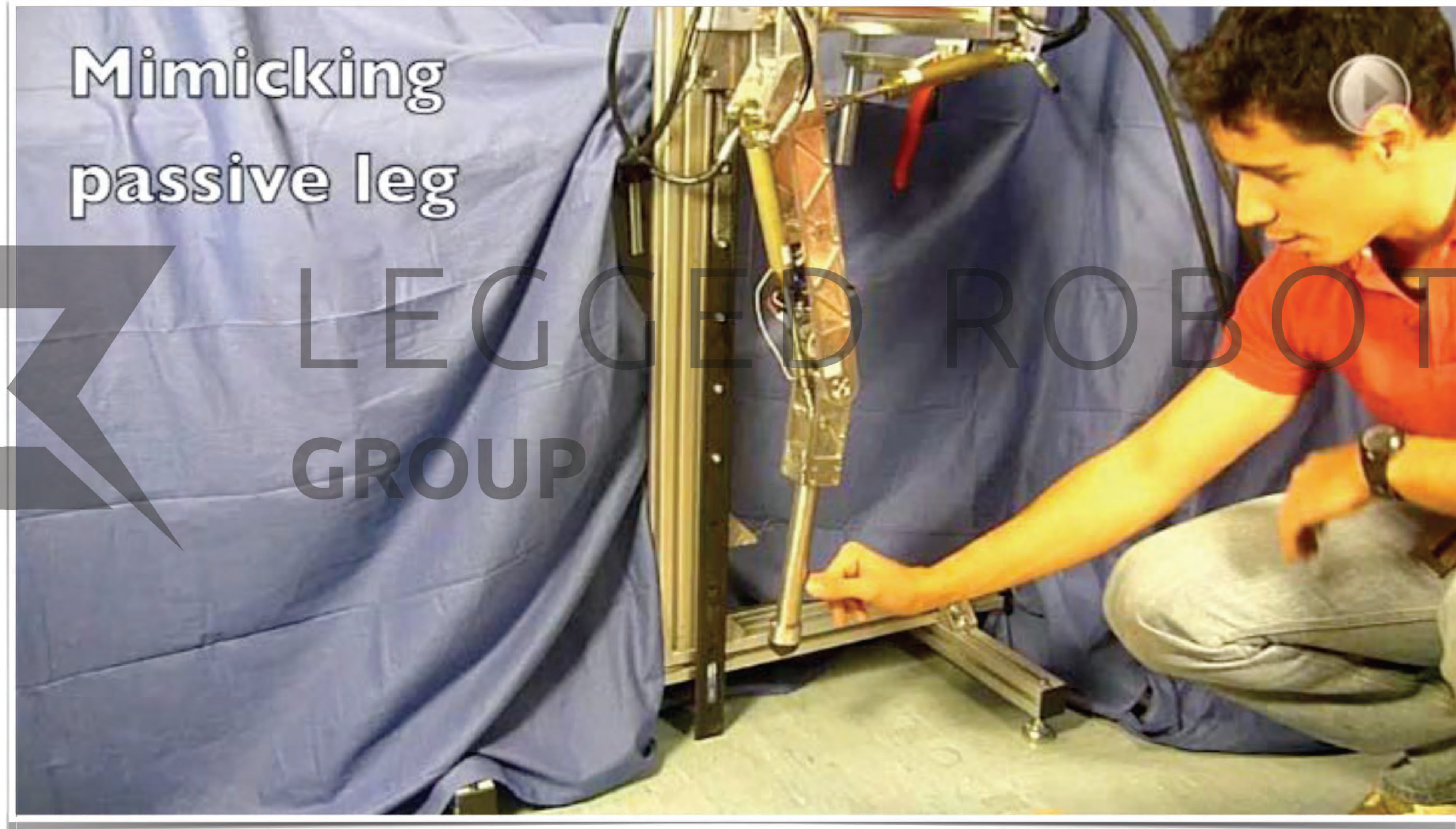
Model-based velocity compensation



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Model-based velocity compensation



Take-home message

controlling
impedance is not
controlling **force**...

... neither controlling
position...

but their **relation**.

Talk on "Interaction Control for Contact Robotics" by Neville Hogan

<https://www.youtube.com/watch?v=GjKy3EFs3g8>

<https://www.youtube.com/watch?v=Dkc1LkTDXXk&t=2693s>

Hogan, N. (1985). Impedance control: An approach to manipulation: Part II—Implementation. *Journal of dynamic systems, measurement, and control*

Hogan N, Buerger S. P. Impedance and interaction control. *Robotics and automation handbook*. 2005;1

Calanca, A., et al. (2016). A review of algorithms for compliant control of stiff and fixed-compliance robots. *IEEE/ASME Transactions on Mechatronics*

Boaventura, T., et al. On the role of load motion compensation in high-performance force control. *IROS*, 2012

Ott, C., Mukherjee, R., & Nakamura, Y. (2010). Unified impedance and admittance control. *ICRA*, 2010, pp. 554-561.



That's all Folks!